

Shear-thickening and the glass transition

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Viscosity changes induced by stirring

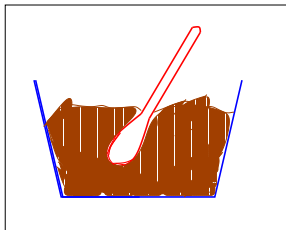
- Shear thinning: blood, paint, ...
- Shear-thickening: corn-starch, talcum mixtures with water.

Structures responsible for viscosities to break upon stirring (i.e. the spatial correlations tend to decrease)

The system tends to move in phase-space, thus becoming more agile

Not surprisingly, shear-thinning is the **rule**, and shear-thickening the **exception**

Stirring-induced glass transition Bertrand, Bibette and Schmitt,
PRE (2002): BiOCl + poly(sodium acrylate)

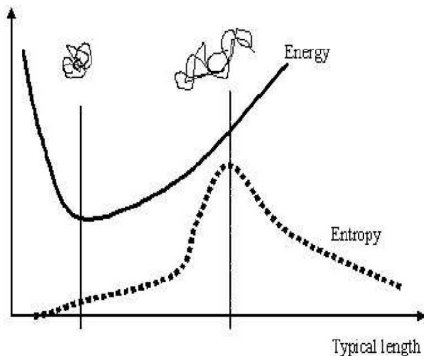


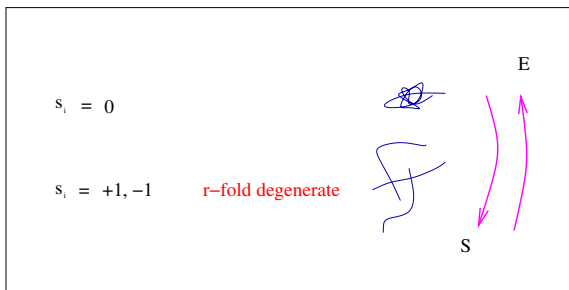
- A theory of (at least this form of) shear-thickening must also be a theory of the glass transition
- To be credible, a theory of the glass transition must naturally incorporate the generic shear-thinning (rejuvenation) phenomena, but also explain when and how shear-thickening happens.

Holmes, Fuchs, Cates, Sollich, Haw: phenomenological theory in the Mode-Coupling format.

Inspiration

A scenario for phase-reentrance: Schupper and Shnerb (2004).
Methyl cellulose in water





$$E = \sum_{ij} J_{ij} s_i s_j + D \sum_i s_i^2$$

disordered interaction + folding term

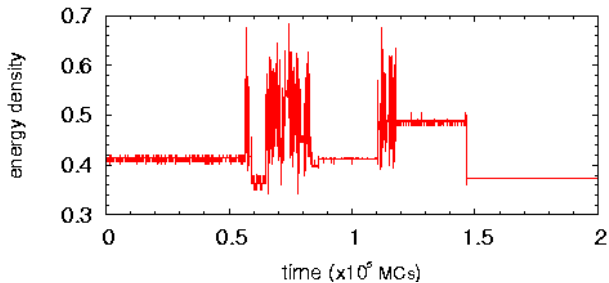
Stirring can play a role similar to entropy
e.g. unfolding polymers (de Gennes (1974))

for example, in this simple model:

$$f_i = \sum_j J_{ij} s_j + 2D s_i + \sigma f_i^{\text{non-conservative}}$$

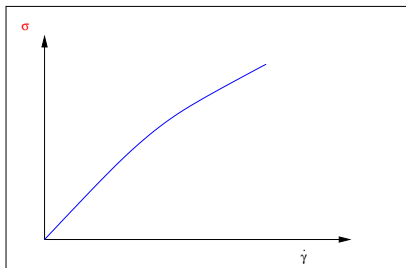
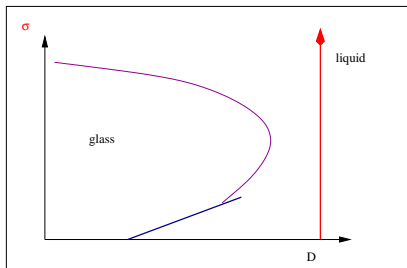
where $f_i^{\text{non-conservative}}$ are forces that do not derive from a potential and hence **do work**.

Jamming with aging



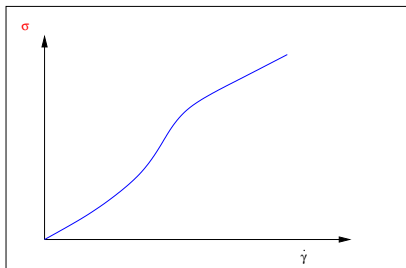
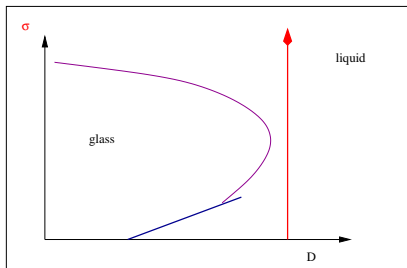
PHASE AND FLOW DIAGRAMS

Shear Thinning



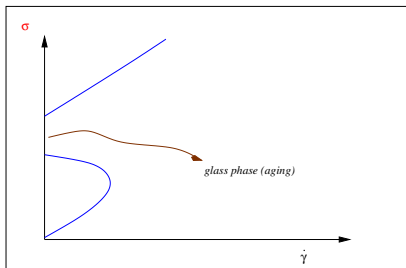
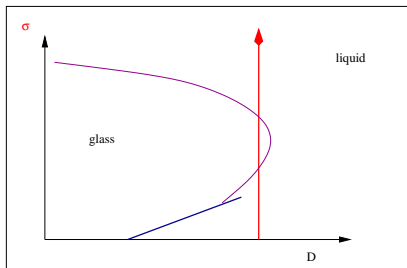
PHASE AND FLOW DIAGRAMS

Shear Thickening



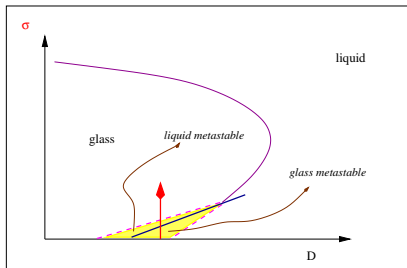
PHASE AND FLOW DIAGRAMS

Second order jamming



PHASE AND FLOW DIAGRAMS

First-order jamming

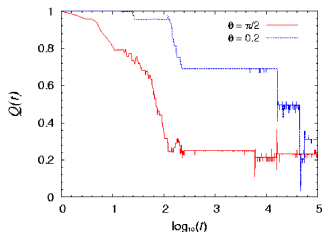
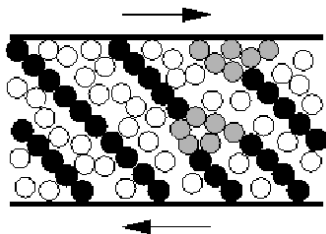


hysteresis

metastable liquid and metastable glass

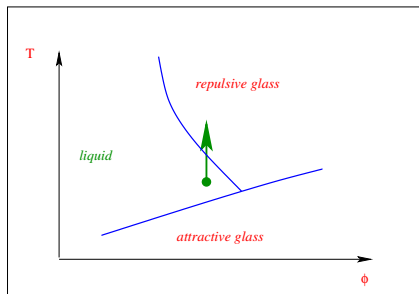
first order ... see Bertrand et al.

Force-chain rearrangements [Cates et al. PRL (1998)]: stirring force changes bring about force-chain rearrangements. **very small changes still induce rearrangements, but these happen slowly.**



Some predictions

- Metastability and hysteresis
- Force-chain rearrangements
- Intermittent behaviour [W.J. Frith et al., J. Rheol. (1996)]
- attractive colloids:



Reichman et al.