

FLUXBRANE INFLATION

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Based on A. Hebecker, S. K., D. Lüst, S. Steinfurt, T. Weigand [arXiv:1104.5016]
and A. Hebecker, S. K., M. Küntzler, D. Lüst, T. Weigand (to appear)

Motivation

- Inflation is one of the crucial concepts in modern cosmology
- Challenge (from particle physics point of view): look for scalar potentials $V(\varphi)$ ($\varphi \equiv$ ‘inflaton’) which satisfy

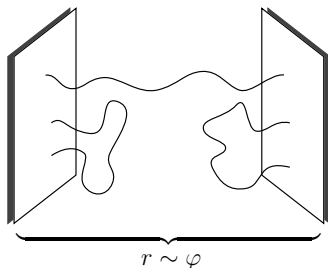
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- Many attempts to construct models of inflation in string theory
- In this talk: Brane Inflation [Dvali, Tye, '98]
- Famous examples:
 - Brane-/Antibrane inflation [Burgess et al., '01; KKLM, '03]
 - D3/D7 inflation with SUSY flux on D7 [Dasgupta et al., '02; Haack et al., '08]
 - ...
- Proposals suffer from η -problem generically:

$$|\eta| \sim \left(\frac{L}{r}\right)^{d_{\perp}} \gg 1$$

($\mathcal{V} = L^6$, $r =$ brane separation, $d_{\perp} =$ codimension)

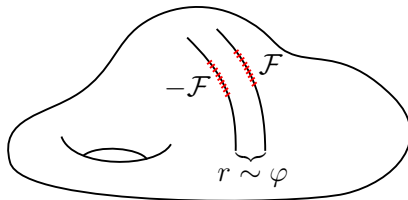
Outline

- 1 Fluxbrane Inflation
- 2 Moduli Stabilisation
- 3 Conclusions & Further Issues

Fluxbrane Inflation

Fluxbrane Inflation: [Hebecker, SK, Lüst, Steinfurt, Weigand, '11]

- Idea: Inflaton = relative deformation modulus of two D7-branes with flux



Fluxbrane Inflation

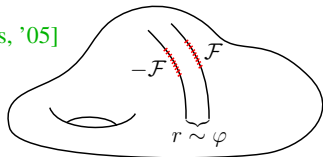
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$$V(\varphi) = \frac{g_{\text{YM}}^2 \xi^2}{2} \left(1 + \alpha \frac{g_{\text{YM}}^2}{16\pi^2} \log \left(\frac{\varphi}{\varphi_0} \right) \right)$$

$$g_{\text{YM}}^2 = \frac{2\pi}{\mathcal{V}_{\text{D7}}}, \quad \xi = \frac{1}{4\pi} \frac{\int_{\text{D7}} J \wedge \mathcal{F}}{\mathcal{V}}, \quad \text{[Jockers, Louis, '05]}$$

$$\alpha = \left(-2 \int_{\text{D7}} \mathcal{F} \wedge \mathcal{F} + \frac{g_{\text{YM}}^2}{2\pi} \left(\int_{\text{D7}} J \wedge \mathcal{F} \right)^2 \right)$$



→ For $\alpha = 1$ we recover the potential of D -term hybrid inflation
 [Binétruy, Dvali, Halyo, '96]

Fluxbrane Inflation - Phenomenology

- Upshot: Naturally flat potential at *large volume*, also for $r \ll L$:

$$\varphi = \frac{r}{2} \sqrt{\frac{g_s \mathcal{V}_{D7}}{\mathcal{V}}} \rightarrow \boxed{|\eta| = \frac{n^2}{2\pi} \frac{1}{(rL)^2} \ll 1} \quad \begin{aligned} \mathcal{V} &= L^6, \mathcal{V}_{D7} = L^4, \\ n &= \# \text{ flux quanta} \end{aligned}$$

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- Spectral index

$$n_s \simeq 1 - \frac{1}{N} \simeq 0.983 \quad \left(\text{WMAP7: } n_s = 0.968, \checkmark \text{ at } 2\sigma \right)$$

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- Amplitude of curvature perturbations (WMAP7: $\frac{v^{3/2}}{v'} = 5.4 \times 10^{-4}$)

$$\rightarrow L \simeq 10, \quad \mathcal{V} \simeq 10^6$$

for *isotropic* compactification manifold

Moduli Stabilisation - Isotropic Large Volume Scenario

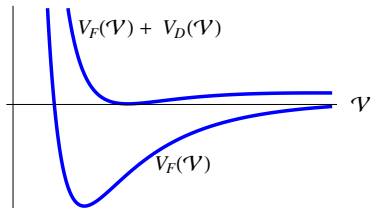
Moduli stabilisation in *isotropic* large volume model with D -term uplift

[Balasubramanian, Berglund, Conlon, Quevedo, Suruliz, '05]

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- $\mathcal{V} \sim \tau_b^{3/2} - \tau_s^{3/2}$, $\tau_b \gg \tau_s$
- Stabilisation through interplay between $\delta K_{\alpha'} \sim \frac{\tilde{\xi}}{\mathcal{V}}$ and $\delta W_{\text{NP}} \sim e^{-a\tau_s}$
- Leading order F - and D -term potential (τ_s integrated out)

$$V_F(\mathcal{V}) \sim \frac{W_0^2}{\mathcal{V}^3} \left(\tilde{\xi} - \log^{3/2} \left(\frac{\mathcal{V}}{W_0} \right) \right), \quad V_D(\mathcal{V}) \sim \frac{n^2}{\mathcal{V}^2}$$



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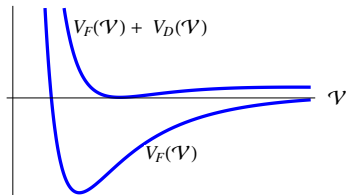
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→ Requires large W_0

- Issues (in *isotropic* model):
 - For $\mathcal{V} \simeq 10^6$ violation of D3-tadpole constraint
 - Parametrically $m_{3/2} \gg m_{\text{KK}}$
 [Discussion with Conlon, Quevedo, ...]
 - Overproduction of cosmic strings, $\xi > \xi_{\text{crit}}$.

→ Consider *anisotropic* model



Moduli Stabilisation - Anisotropic Large Volume Scenario

Moduli stabilisation in *anisotropic* large volume model

[Cicoli, Conlon, Quevedo, '08]

- We consider

$$\mathcal{V} = \frac{1}{3!} \kappa_{111} t_1^3 + \frac{1}{2} \kappa_{122} t_1 t_2^2 + \frac{1}{3!} \kappa_{sss} t_s^3, \quad t_1 \gg t_2 \gg t_s$$

- Ratio $x \equiv t_1/t_2$ fixed by interplay between δK_{g_s} [Berg et al., '05] and D -term

$$\delta V_{g_s} \sim \frac{W_0^2}{\mathcal{V}^3 \mathcal{V}^{1/3}} x^2, \quad V_D \sim \frac{n^2}{\mathcal{V}^2} \frac{1}{x}$$

Moduli Stabilisation - Anisotropic Large Volume Scenario

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- Upshot: [Hebecker, SK, Küntzler, Lüst, Weigand, '12]
 - Allows for smaller W_0 (compared to isotropic model)
 - D3-tadpole constraint can be satisfied
 - $m_{3/2} \ll m_{\text{KK}}$
 - Cosmic string bound satisfied

Conclusions & Further Issues

Fluxbrane Inflation:

- Model of stringy D -term hybrid inflation
- Attractive phenomenology (large volume, n_s , cosmic strings)
- Stabilisation of Kähler moduli in anisotropic large volume scenario
- Uplift via D -term possible

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Next step: investigate higher order inflaton mass corrections

Brane modulus (= inflaton) enters:

- Superpotential $W \rightarrow$ Flux choice
[work with M. Arends, A. Hebecker, K. Heimpel, C. Schick, T. Weigand]
- Kähler potential $K = -\log(S + \bar{S} - k(\varphi, \bar{\varphi}))$ [Jockers, Louis, '04, '05]
 \rightarrow Shift-symmetries (e.g. $K3 \times K3$)
- String loop corrections $\delta K_{g_s}(\varphi, \bar{\varphi})$ [Berg, Haack, Körs, Pajer, '05, '07]