

Orientifolds and new $\mathcal{N} = 1$ dualities

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Motivation

Why hunt for [4d $\mathcal{N} = 1$] gauge theory dualities?

- Understand gauge theories at strong coupling
- Unlike AdS/CFT, finite N !
- Useful for phenomenology
- Better understanding of string theory

Invitation: Montonen-Olive duality ($\mathcal{N} = 4$)

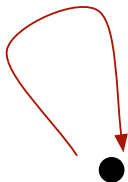
N D3's

●
 $SU(N)$

Invitation: Montonen-Olive duality ($\mathcal{N} = 4$)

$SL(2, Z)$ self-duality

N D3's

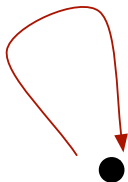


$SU(N)$

$$\tau \rightarrow \frac{a\tau + b}{c\tau + d}$$

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N D3's



Type IIB String Theory:
Exact $SL(2, Z)$ S-duality
(D3 invariant)

Invitation: $\mathcal{N} = 4$ orientifold dualities

N D3's + O3



$SO(2N)$



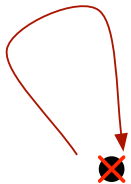
$SO(2N+1)$



$USp(2N)$

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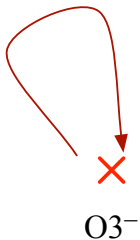
S-dual



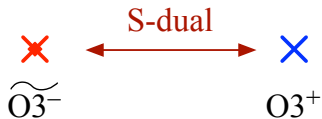
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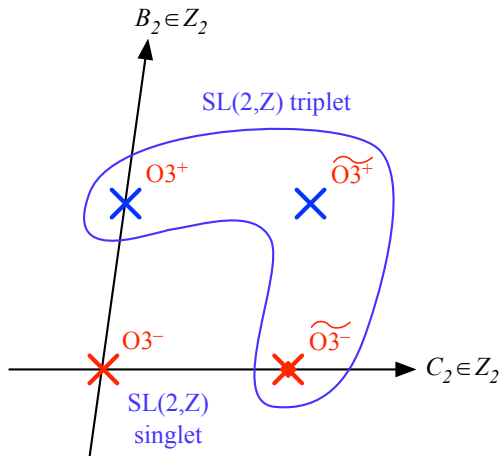
$SL(2, \mathbb{Z})$ invariant



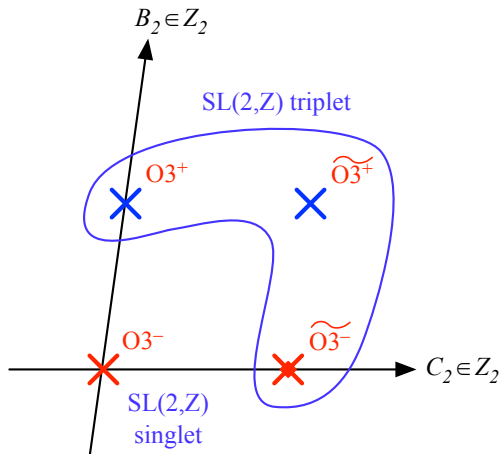
$O3$



Invitation: $\mathcal{N} = 4$ orientifold dualities



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$$H^3(S^5/\mathbb{Z}_2, \widetilde{\mathbb{Z}}) = \mathbb{Z}_2$$

Strategy

- D3 branes $SL(2, \mathbb{Z})$ invariant
- Orientifolds may break $SL(2, \mathbb{Z})$
- Can lead to gauge theory S-dualities

Flat background ($\mathcal{N} = 4$)

What about D3's at Calabi-Yau singularity ($\mathcal{N} = 1$)?

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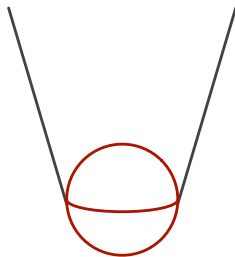
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What about D3's at Calabi-Yau singularity ($\mathcal{N} = 1$)?

del Pezzo 0

“Simplest” $\mathcal{N} = 1$ singularity: $\mathbb{C}^3/\mathbb{Z}_3$ ($z^i \rightarrow e^{2\pi i/3} z^i$)

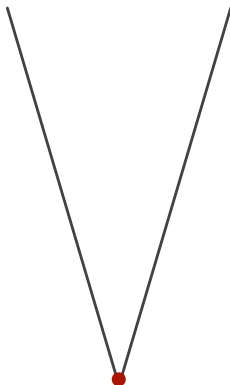
Calabi-Yau cone over $dP_0 = \mathbb{CP}^2$



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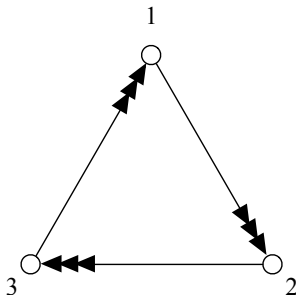
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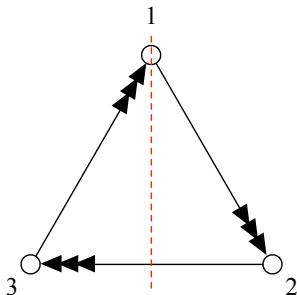


$$W = \epsilon_{ijk} X_{12}^i X_{23}^j X_{31}^k, \quad \text{SU}(3) \times \text{U}(1)_R \text{ global symm.}$$

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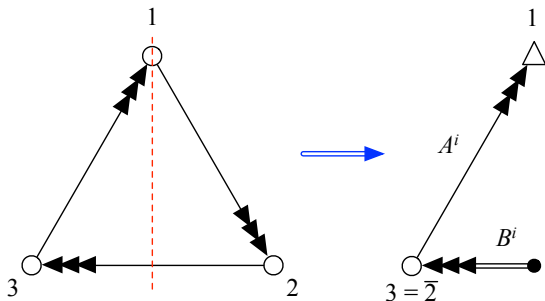


$\sigma : z^i \rightarrow -z^i$ (Compact O7 plane)

del Pezzo 0

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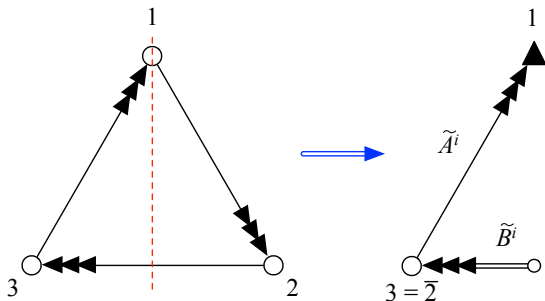


$$W = \frac{1}{2} \epsilon_{ijk} A^i A^j B^k, \quad \text{SU}(3) \times \text{U}(1)_R \text{ global symm.}$$

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$$W = \frac{1}{2} \epsilon_{ijk} \tilde{A}^i \tilde{A}^j \tilde{B}^k, \quad \text{SU}(3) \times \text{U}(1)_R \text{ global symm.}$$

The orientifolds

	$SO(N-4)$	$SU(N)$	$SU(3)$	$U(1)_R$	\mathbb{Z}_3
A^i	\square	$\bar{\square}$	\square	$\frac{2}{3} + \frac{2}{N}$	ω_{3N}
B^i	1	\square	\square	$\frac{2}{3} - \frac{4}{N}$	ω_{3N}^{-2}

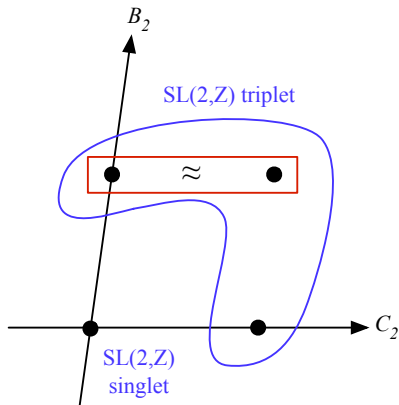
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	$Sp(\tilde{N}+4)$	$SU(\tilde{N})$	$SU(3)$	$U(1)_R$	\mathbb{Z}_3
\tilde{A}^i	\square	$\bar{\square}$	\square	$\frac{2}{3} - \frac{2}{\tilde{N}}$	$\omega_{3\tilde{N}}$
\tilde{B}^i	1	\square	\square	$\frac{2}{3} + \frac{4}{\tilde{N}}$	$\omega_{3\tilde{N}}^{-2}$

$$W = \frac{1}{2} \epsilon_{ijk} \tilde{A}^i \tilde{A}^j \tilde{B}^k$$

A duality?

Is there a similar story to before? $H^3(S^5/\mathbb{Z}_6, \tilde{\mathbb{Z}}) = \mathbb{Z}_2$



Anomaly matching

Check hypothesis using 't Hooft anomaly matching

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$SO(N - 4) \times SU(N)$ theory:

$SU(3)^3$	$\frac{3}{2}(N - 3)N$
$SU(3)^2 \times U(1)_R$	$-\frac{1}{2}(N - 3)N - 6$
$U(1)_R^3$	$\frac{4}{3}(N - 3)N - 33$
$U(1)_R$	-9

$Sp(\tilde{N} + 4) \times SU(\tilde{N})$ theory:

$SU(3)^3$	$\frac{3}{2}\tilde{N}(\tilde{N} + 3)$
$SU(3)^2 \times U(1)_R$	$-\frac{1}{2}\tilde{N}(\tilde{N} + 3) - 6$
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Anomaly matching

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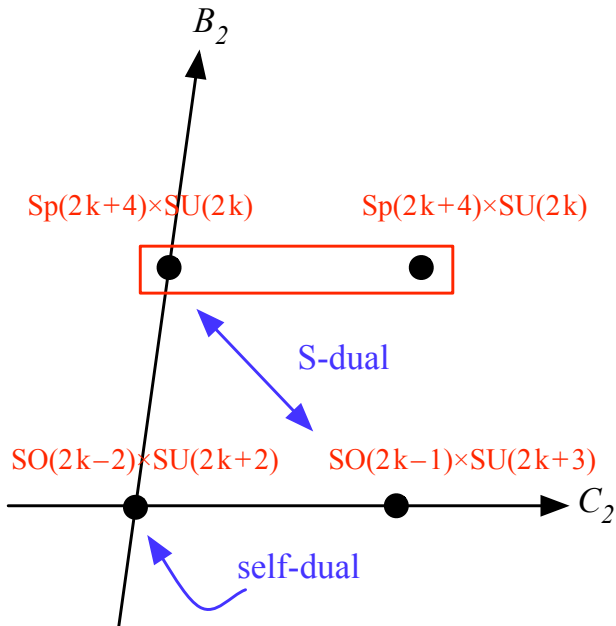
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Anomalies match for $\tilde{N} = N - 3$!



Moduli space

- Mesons match: $(AAB)^n \longleftrightarrow (\tilde{A}\tilde{A}\tilde{B})^n$
- Baryons of lowest possible R-charge:

① $B^N, Q_R = \frac{2(N-6)}{3}, Q_3 = \omega_3$

② $\tilde{A}^{\tilde{N}}, Q_R = \frac{2(\tilde{N}-3)}{3}, Q_3 = \omega_3$

$$B^N \longleftrightarrow \tilde{A}^{\tilde{N}}$$

$$\frac{2(N-6)}{3} = \frac{2(\tilde{N}-3)}{3} \longrightarrow N = \tilde{N} + 3$$

D3 charge

- Q_{D3} is $SL(2, \mathbb{Z})$ invariant \rightarrow same for dual theories
- Compute using exceptional collections
- Get $Q_{D3} = N/2 - 3/4$, $\tilde{Q}_{D3} = \tilde{N}/2 + 3/4$
- Reproduces the rank relation $\tilde{N} = N - 3$ again

N -dependent checks

(1) $SU(5) \longleftrightarrow Sp(6) \times SU(2)$

- Both have runaway vacuum
- No quantum moduli space to match

N -dependent checks

$$(2) \text{SO}(3) \times \text{SU}(7) \longleftrightarrow \text{Sp}(8) \times \text{SU}(4)$$

- $\text{Sp}(8)$ s-confines, Seiberg dualize $\text{SU}(4) \cong \text{SO}(6)$
- Free IR fixed point
- Quantum moduli space: \tilde{A}^4 (w/ constraint)

- Turn on controlled vevs and compare with $\text{SO}(3) \times \text{SU}(7)$
- Some nontrivial checks... work in progress

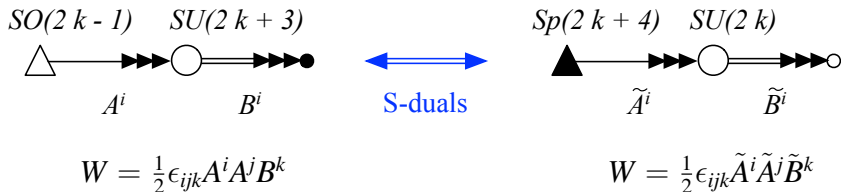
N -dependent checks

(3) Higher N

Expect:

- Quantum moduli space: mesonic and baryonic directions
- Interacting IR fixed point
- Difficult to check. . .

Summary



- [Many] nontrivial checks
- Novel duality from gauge theory perspective
- “Cousin” of well known $SO(2k+1) \leftrightarrow Sp(2k) \mathcal{N} = 4$ duality

Conclusions

- Orientifolds can break $SL(2, \mathbb{Z})$, lead to S-dual theories
- Interesting new dualities from $\mathcal{N} = 1$ orientifold singularities
- $\mathbb{C}_3/\mathbb{Z}_3$ merely the simplest example of anomaly matching

Iñaki's talk:

- Superconformal index
- Construction of gauge theory using fractional branes
- Orientifold transition

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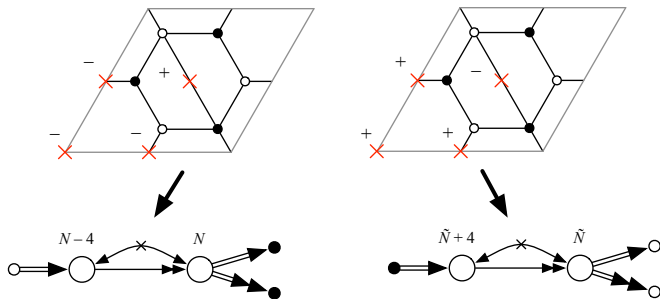
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Backup slides

Example II

First del Pezzo:

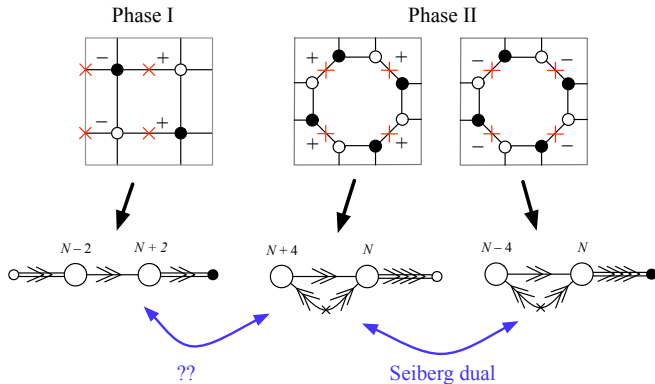


Anomalies match for $\tilde{N} = N - 2$, odd N .

Even N : moduli space mismatch

Example III

Zeroth Hirzebruch ($\mathbb{P}_1 \times \mathbb{P}_1$).



Anomalies match for all N ; spectra do not match for even N

Exact duality?

Is the duality exact?

- Hard to answer in field theory
- Beta functions: $(b_{SO}, b_{SU}) = (-18, 9)$, $(b_{Sp}, b_{SU}) = (9, -9)$
- \longrightarrow effective field theory between Λ_{IR} and Λ_{UV}
- Not easy to check whether dual theories different in the UV
- Have to go back to string theory...