

# Microstructure for continuous and localised intrinsic curvature creation

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## Abstract

Nematic elastomers and glasses hugely and reversibly contract/elongate parallel/perpendicular to their directors under heating or illumination. With uniform directors and as slender sheets, they can pull with huge load-to-weight ratios, but cannot push because of Euler instabilities.

For complex tasks at small scales, the material must be the machine itself<sup>1</sup>. We show how to design continuous, non-uniform director fields enable flat sheets to develop intrinsic curvature<sup>2,3</sup>, that is mostly continuously distributed, and thereby adopt complex shapes. Likewise, piecewise-continuous fields give Gaussian curvature localised at points<sup>4</sup>, much as origami folding of paper does. But in this case the “origami” is instead non-isometric<sup>5</sup>.

Blocking emerging non-developable surfaces causes stretch away from the new metric and the response can be strong pulling, and strong pushing<sup>6</sup> without Euler failures. New micromechanical possibilities arise.

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<sup>1</sup> K. Bhattacharya and R.D. James, *Science* **307**, 53-54 (2005)

<sup>2</sup> C.D. Modes, K. Bhattacharya and M Warner, *Phys. Rev. E* **81**, 060701(R) (2010)  
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<sup>3</sup> C. Mostajeran, M. Warner, T.H. Ware and T.J. White, *Proc. Roy. Soc.*, **A472**, 20160112 (2016)  
& *Proc. R. Soc. A* **20170566** (2017)

<sup>4</sup> CD Modes and M Warner, *Phys. Rev. E* **84**, 021711 (2011)  
& *SPIE* **8279**, 82790Q-82790Q-8 (2012)

<sup>5</sup> P. Plucinsky, M. Lemm and K. Bhattacharya, *Phys. Rev. E* **94**, 010701(R) (2016)

<sup>6</sup> T.J. White and group, private communication.