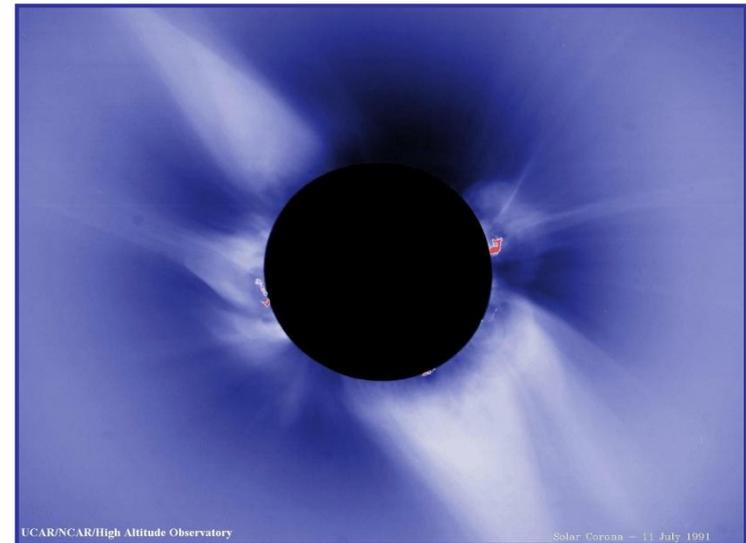


Observational evidence for anisotropic solar wind turbulence on fluid and kinetic scales

Tim Horbury
Imperial College London

Thanks to Chris Chen, Robert Wicks, Alex Schekochihin, Miriam Forman

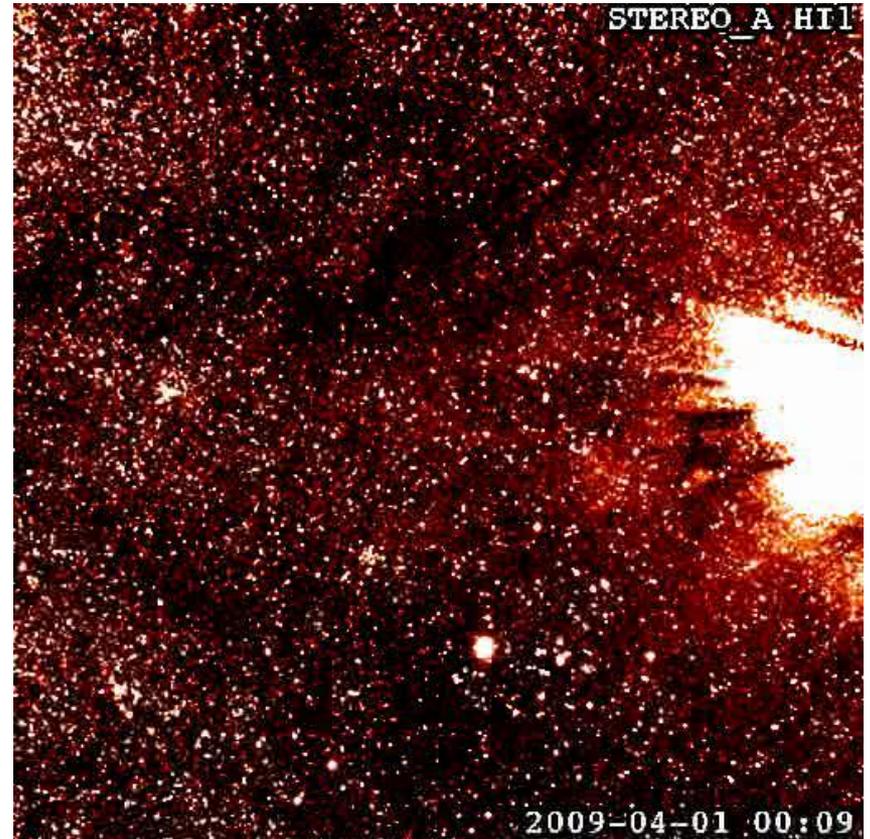
- The solar wind as a turbulence laboratory
- What we know: the basics
- MHD scale cascade
- Ion scale cascade
- Kinetics: instabilities
- Open questions



What is the solar wind?

- Collisionless, magnetised plasma
- Continual, but variable, outflow from Sun's corona
- Carries waves and turbulence from corona

- **Complex** due to solar variability, solar rotation, and in situ processes
- **Variable** on all measured scales, from sub-second → centuries



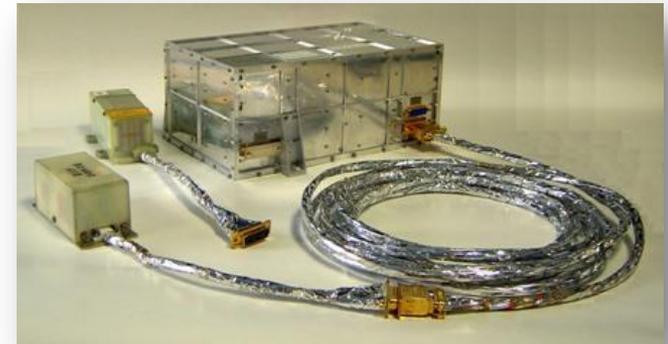
STEREO/HI

Typical solar wind parameters (near Earth)

| | |
|------------------------|--|
| Composition | Mostly protons, few percent alpha, small heavies |
| Ion temperature | $\sim 10^5$ K |
| Bulk speed | 250-800 km/s |
| Alfven speed | ~ 40 km/s |
| Debye length | ~ 10 m |
| Mean free path | ~ 1 AU |
| Proton gyroradius | ~ 100 km |
| Proton inertial length | ~ 100 km |
| Magnetic field | ~ 5 nT |
| Proton beta | ~ 1 |

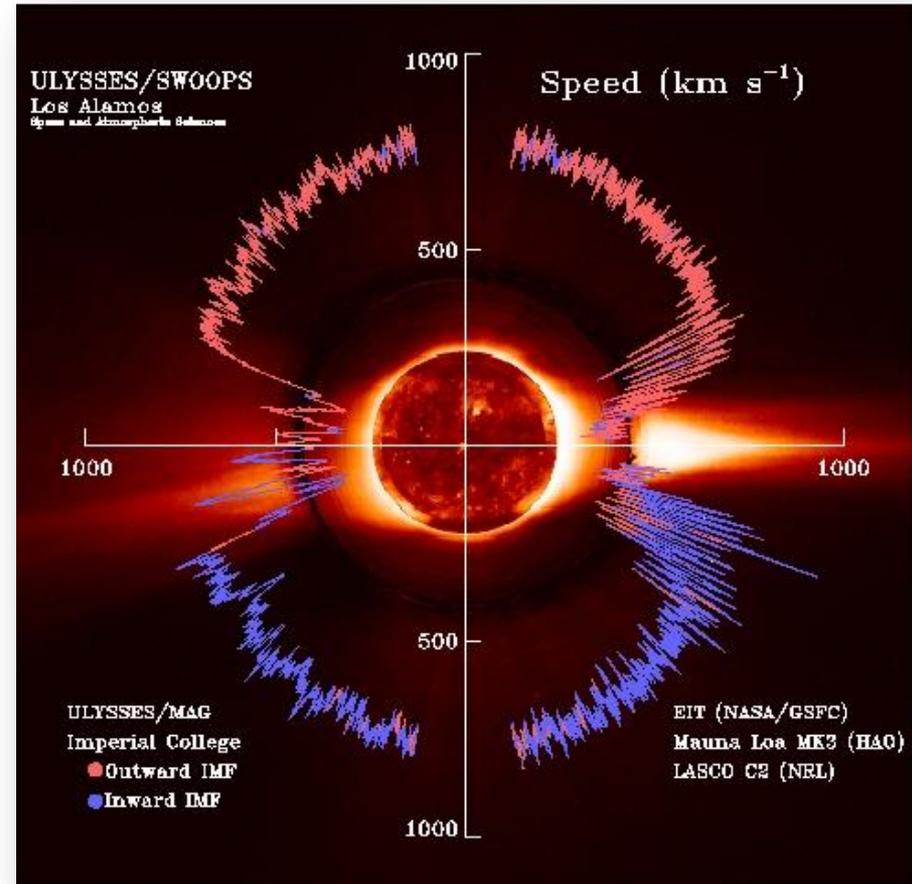
Spacecraft as sensors

- Spacecraft are (mostly) test particles
- Natural fields are very small – significant spacecraft interference issues
- Typical measurements
 - Magnetic field (DC to tens Hz)
 - Electric field
 - Bulk ion properties (velocity, temperature, density)
 - Bulk electron properties (velocity, temperature, density)
 - Full plasma distributions including composition
 - Energetic particles



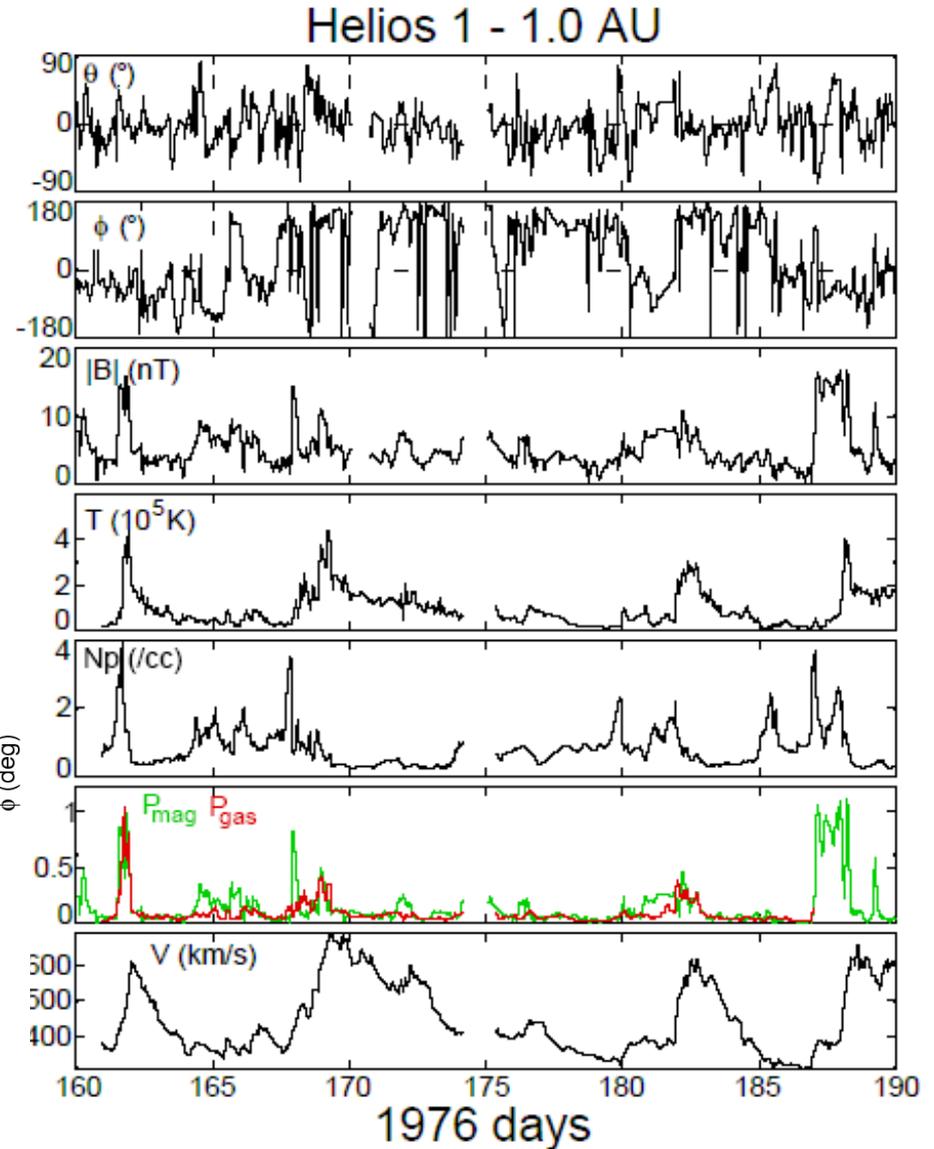
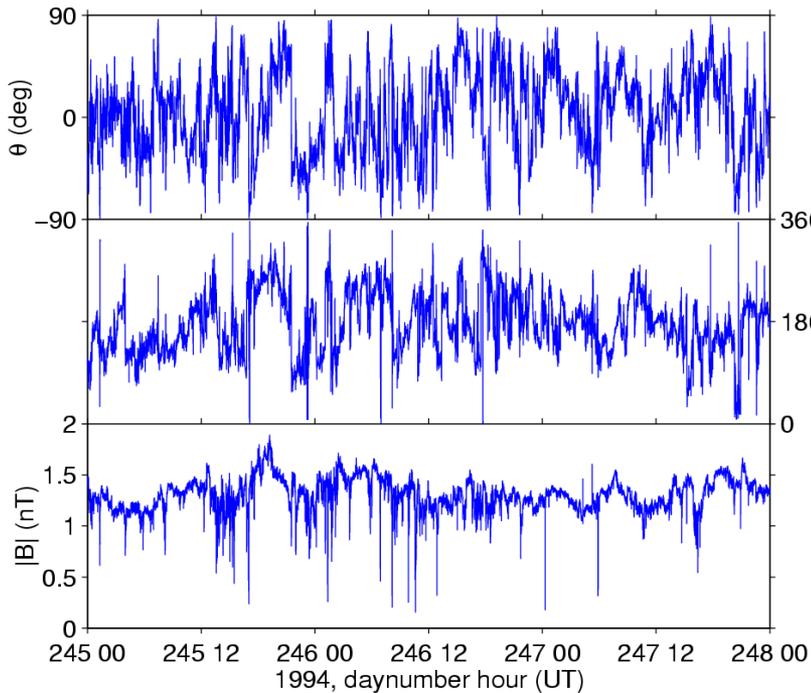
Exploring the solar system

- Spacecraft have explored most of the solar system
- None has a fully comprehensive instrument package
- Big changes in properties with distance, latitude, solar cycle
- Biggest factor is fast vs slow solar wind



Typical conditions at 1.0 AU

- Individual streams last a few days
- Always need to consider the context



Interpreting spacecraft measurements

- In the solar wind (usually),

$$V_A \sim 50 \text{ km/s}, V_{SW} > \sim 300 \text{ km/s}$$

- Therefore,

$$V_{SW} \gg V_A$$

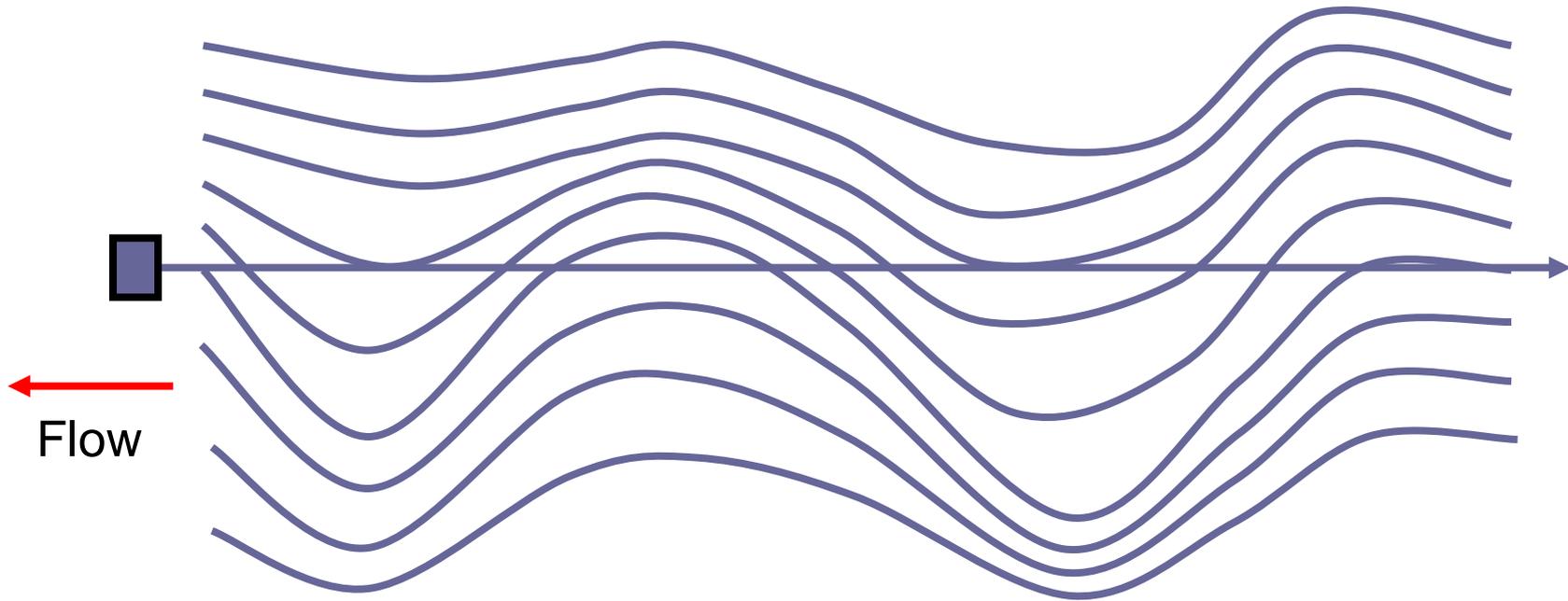
- **Taylor's hypothesis:** time series can be considered a spatial sample
- We can convert spacecraft frequency f into a plasma frame wavenumber k :

$$k = 2\pi f / V_{SW}$$

- Almost always valid in the solar wind
- Makes analysis much easier
- Not valid in, e.g. magnetosheath, upper corona, kinetic scales(?)

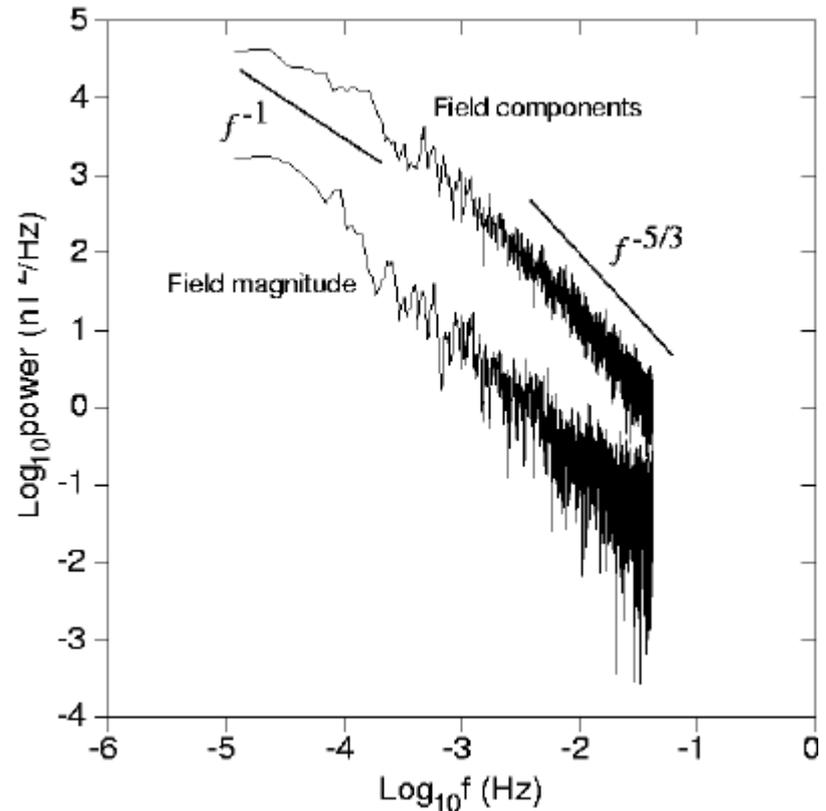
Interpreting spacecraft measurements

- Solar wind flows radially away from Sun, over spacecraft
- Time series is a one dimensional spatial sample through the plasma
- Measure variations along one flow line



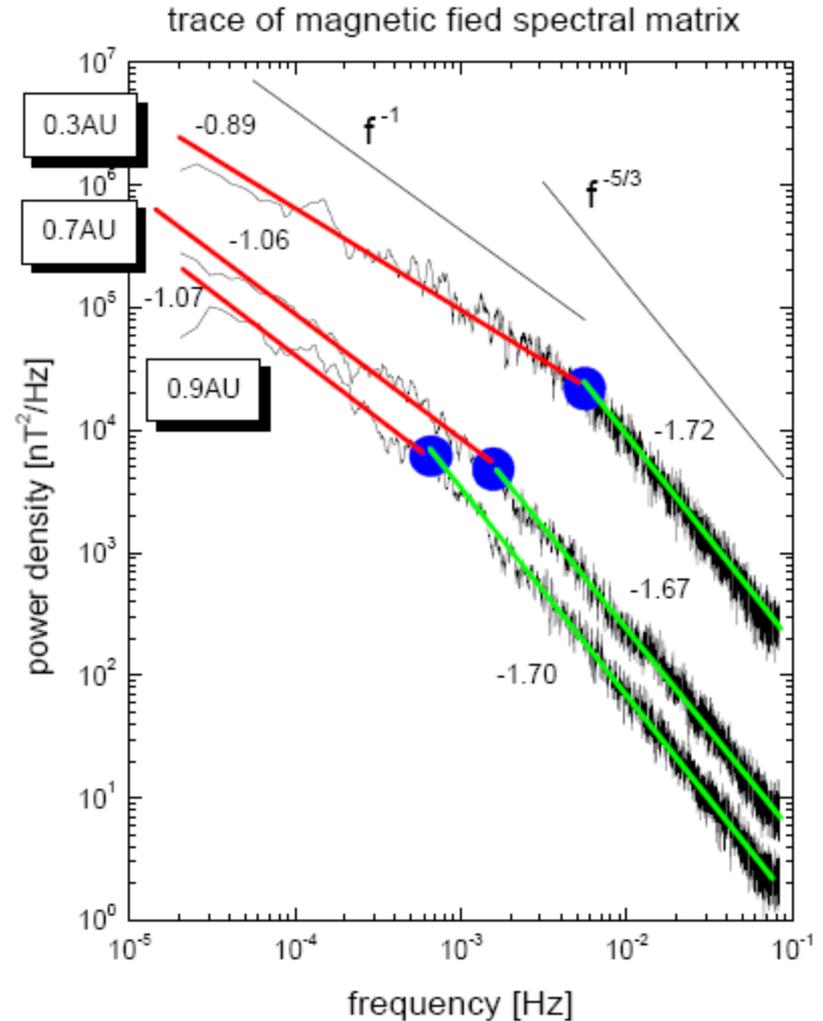
Things we know: power spectrum

- Extended fluid scale inertial range
- Magnetic field power spectrum:
 - $f^{-5/3}$
- Inertial range covers $\sim 10^2$ in scale
- Components much higher power than magnitude
 - Largely non-compressive



Active turbulent cascade in fast wind

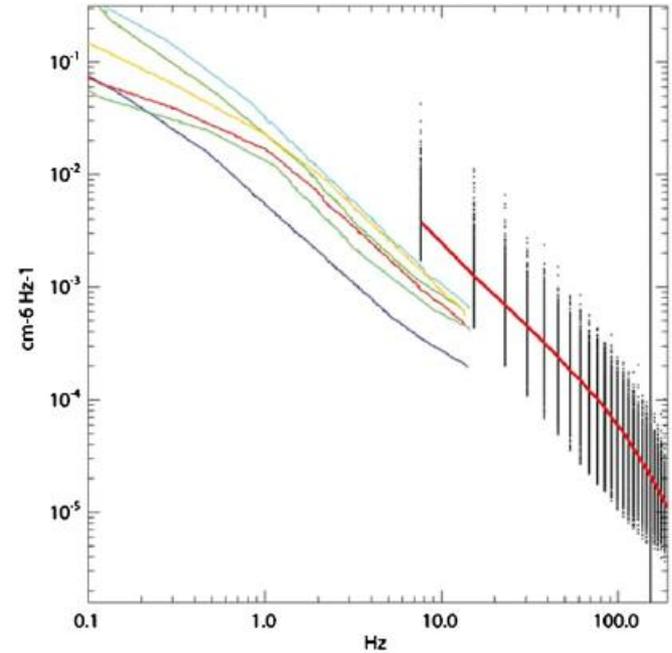
- Bavassano et al (1982)
- Fast wind: “knee” in spectrum
- Spectrum steepens further from the Sun
- Evidence of energy transfer between scales: **turbulent cascade**



after Bavassano et al 1982

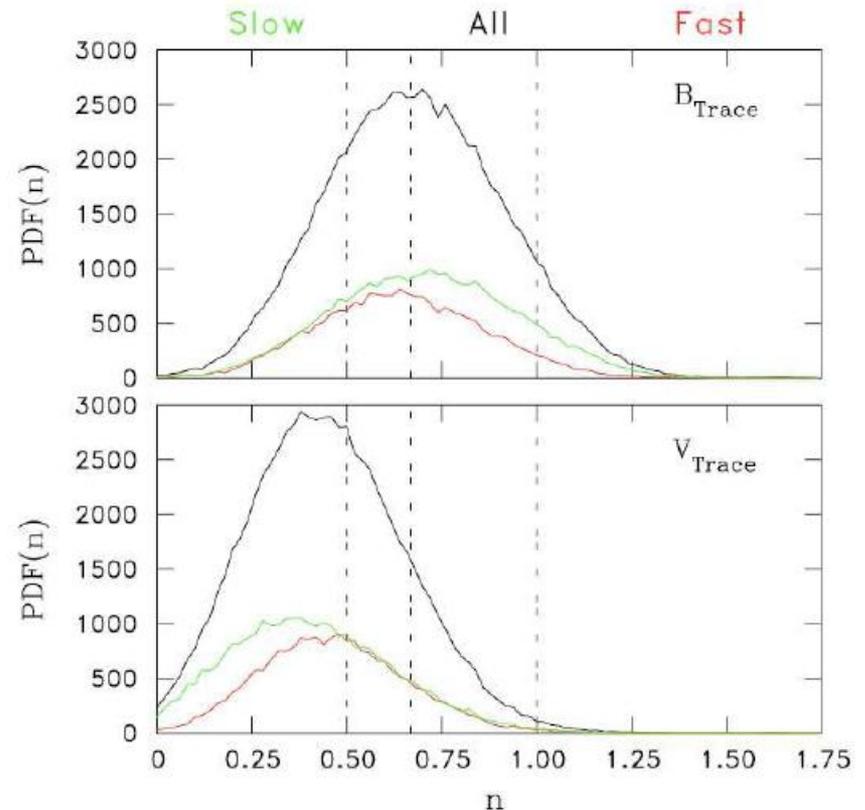
Density spectrum

- Malaspina et al., Ap. J., v.711, 322, 2010
- See also Celnikier et al., Astron. Astrophys., v.181, 138, 1987
- Broadband density spectrum
- Evidence for break at ion gyroscale
- Behaviour as a passive scalar on MHD scales?



Velocity vs magnetic field scaling

- Magnetic field has $5/3$ spectral index
- Velocity has $3/2$ spectral index (Podesta, 2009)
- Physical cause of this effect?
 - Related to Alfvénicity?



Tessein et al., 2009

Alfvén waves

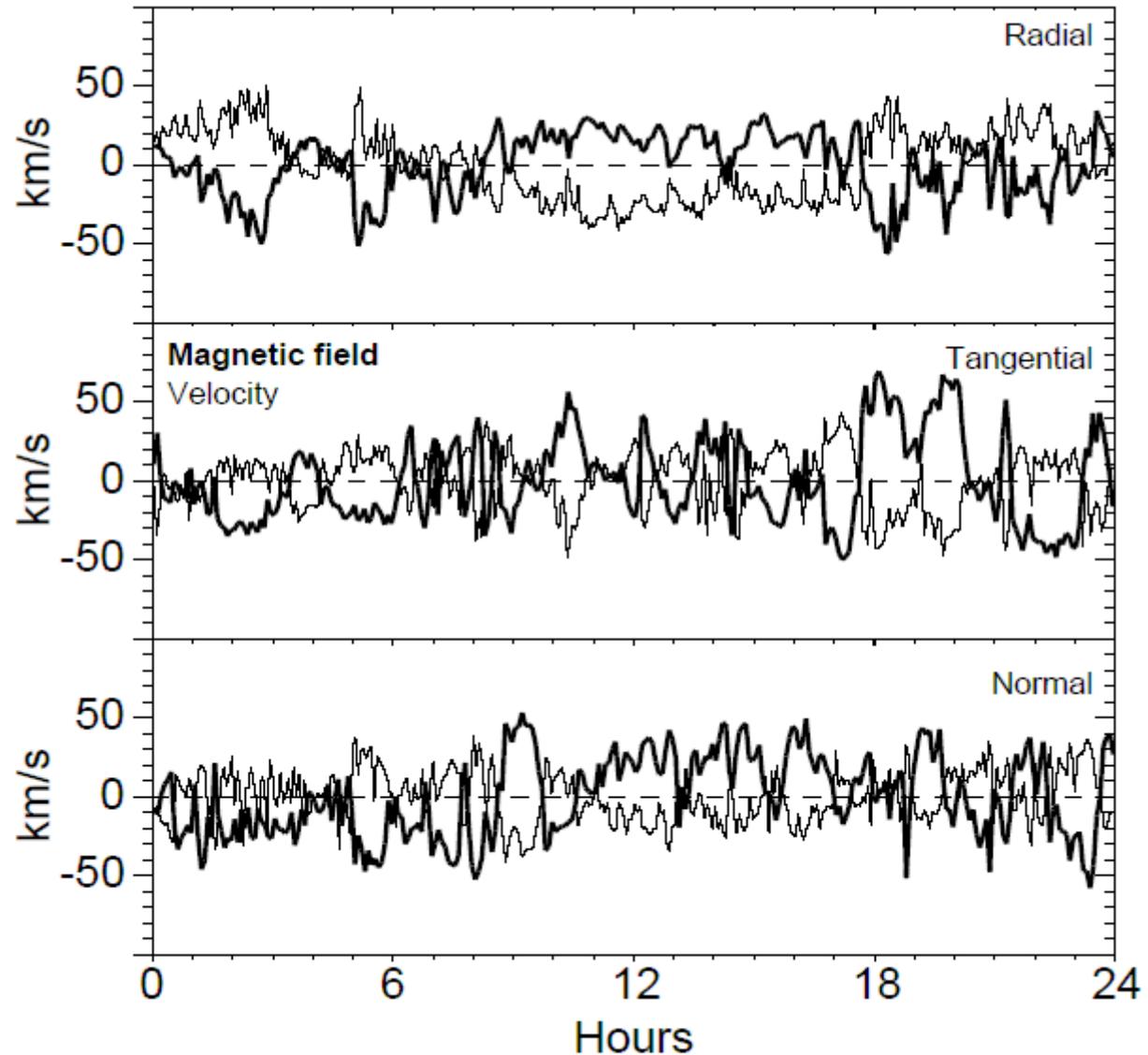
Field-parallel Alfvén wave:

- B and V variations anti-correlated

Field-anti-parallel

Alfvén wave:

- B and V variations correlated
- See this very clearly in the solar wind
- Most common in high speed wind



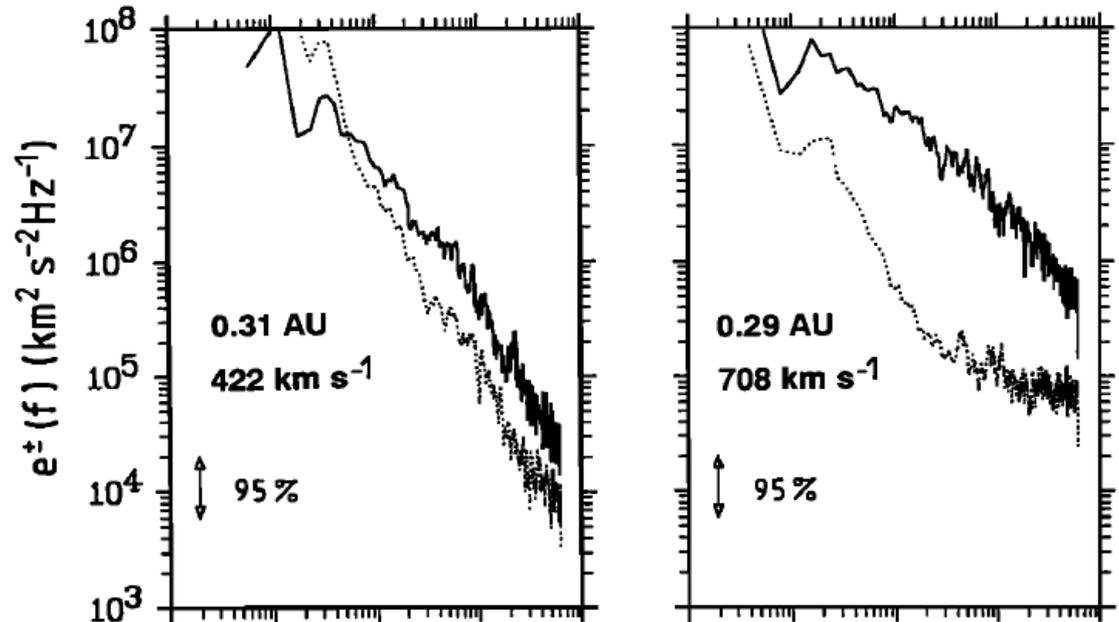
Elsasser variable power spectra

Fast wind

- Imbalanced, dominant outward component
- “Diamond” spectrum

Slow wind

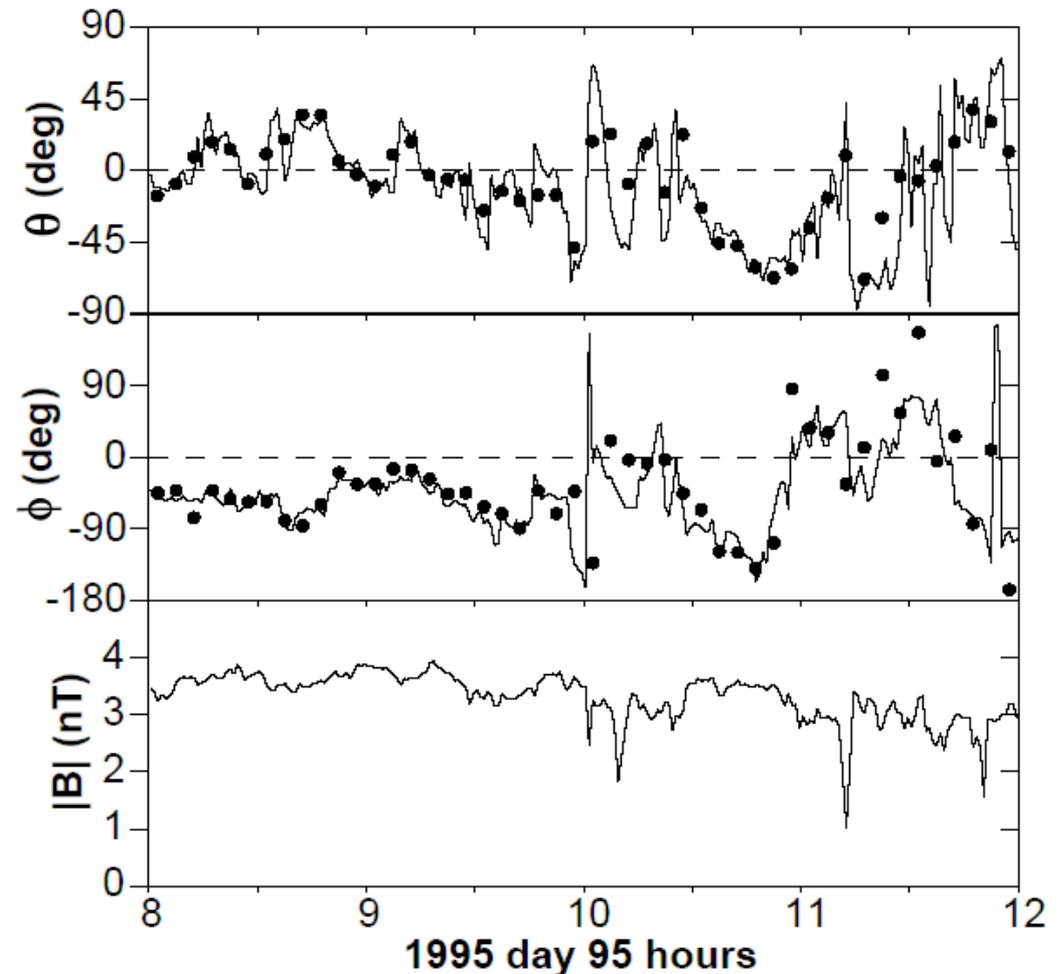
- More balanced on average
- Longer inertial range
- **Solar wind often shows significant imbalance**



Marsch and Tu, JGR, 1990

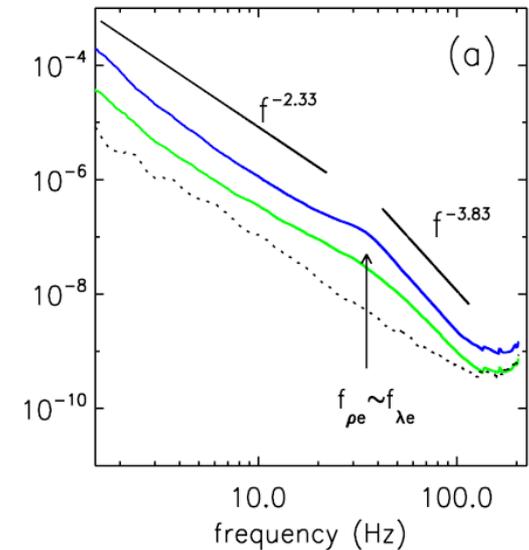
Field-aligned anisotropy

- Power levels tend to be perpendicular to local magnetic field direction
→ **anisotropy**
- Dots: local minimum variance direction
- Track large scale changes in field direction
- Small scale turbulence “rides” on the back of large scale waves

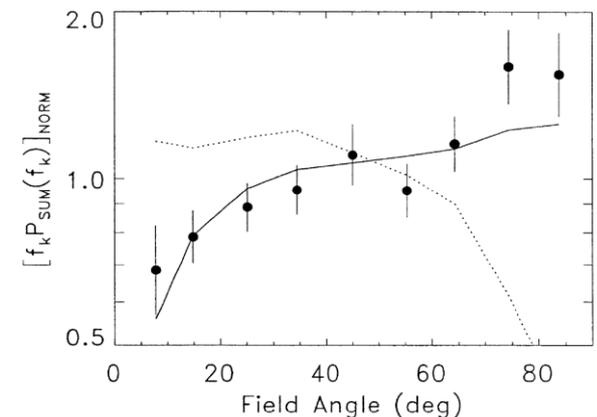


Types of anisotropy

- Variance anisotropy
 - $\delta B_{\perp} > \delta B_{\parallel}$ (e.g. Belcher and Davis, 1971)
- Wavevector anisotropy
 - Different energy in wavevectors in different directions (e.g. Bieber et al., 1996)
- Scaling anisotropy
 - Different power laws in different directions
- Anisotropy of energy transfer
 - Turbulent cascade can have different rates in different directions
- “Imbalance”
 - Parallel/anti-parallel propagation of Alfvénic turbulence



Sahraoui et al., 2009

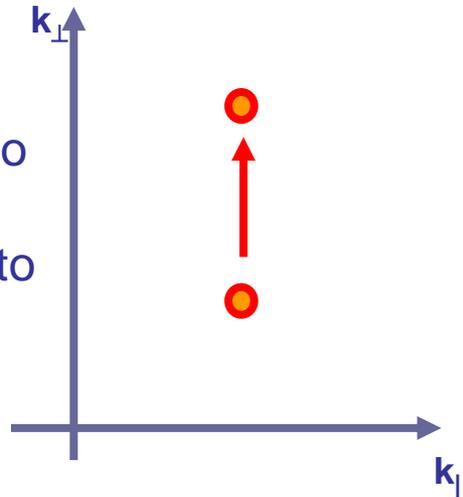


Bieber et al., 1996

Anisotropic energy transfer

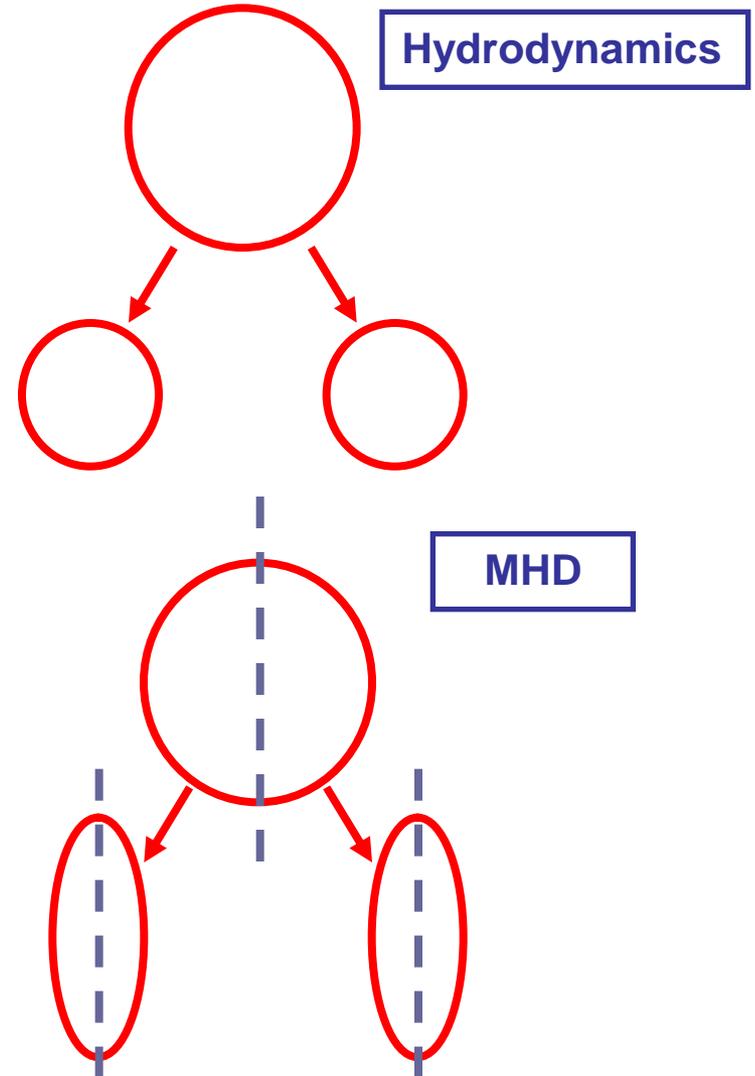
Wavevectors

- Energy tends to move perpendicular to magnetic field



Eddies

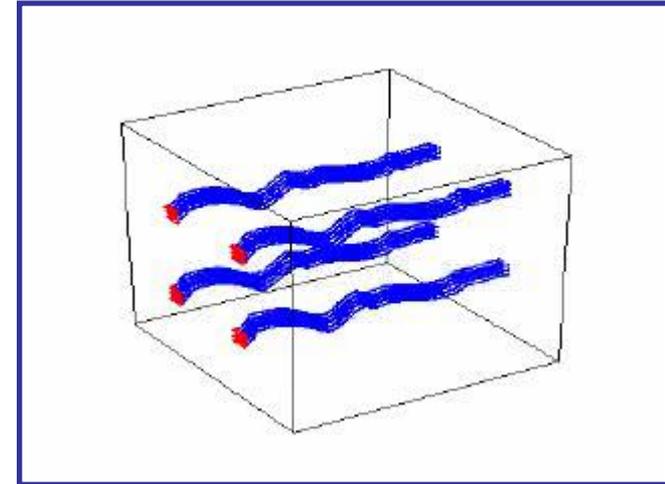
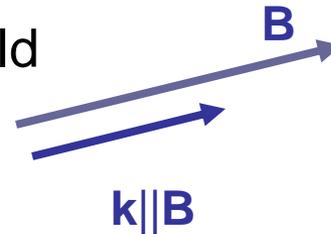
- On average, tend to become smaller perpendicular to field
- Results in long, fine structures along the magnetic field



Anisotropy and 3D magnetic field structure

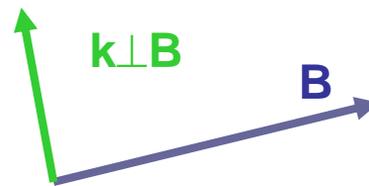
Slab

- Plane waves
- Infinite correlation length perpendicular to magnetic field
- Flux tubes stay together

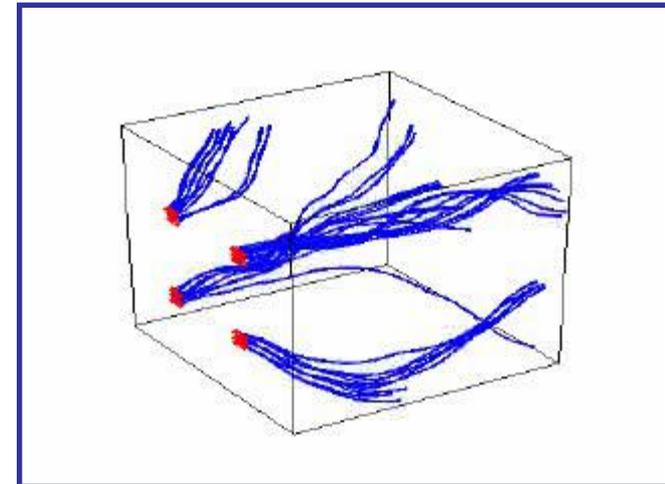


2D (+slab)

- Finite perpendicular correlation length
- Flux tubes “shred”

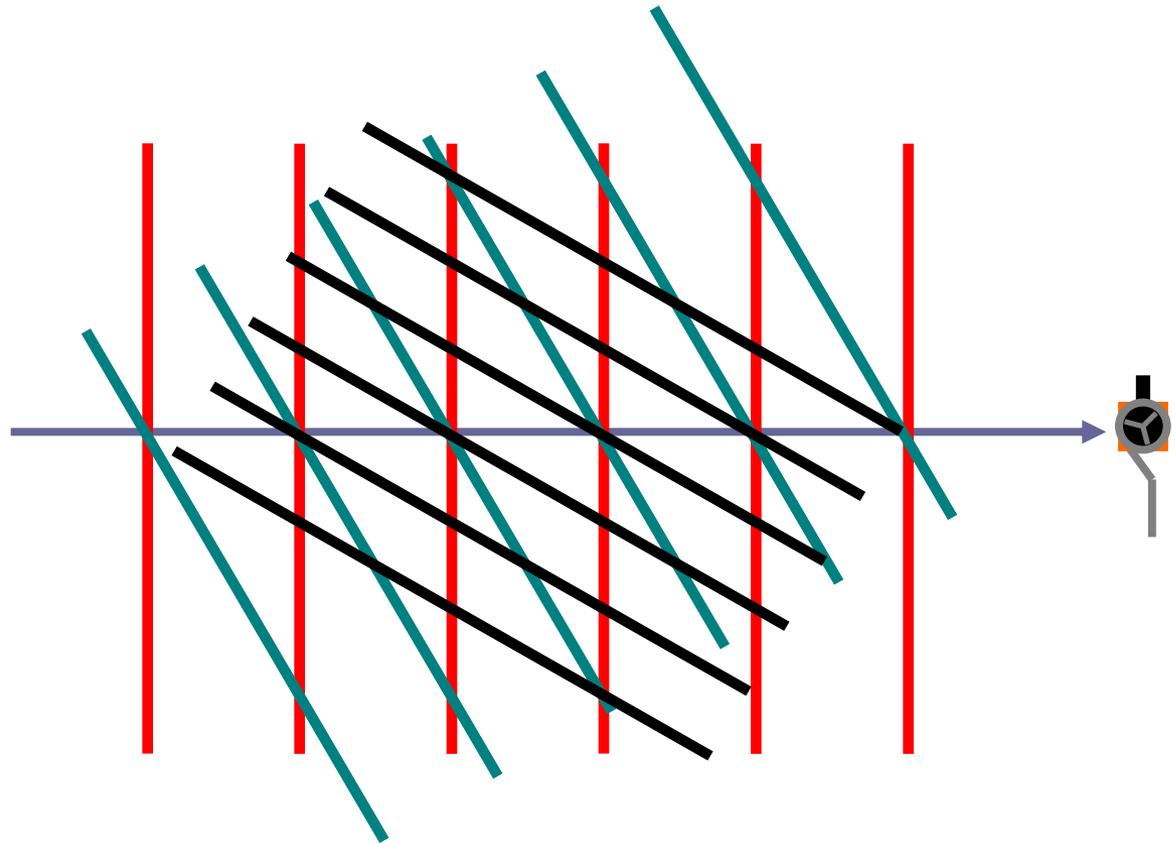


→ Important consequences for particle transport



Measuring anisotropy: reduced spectrum

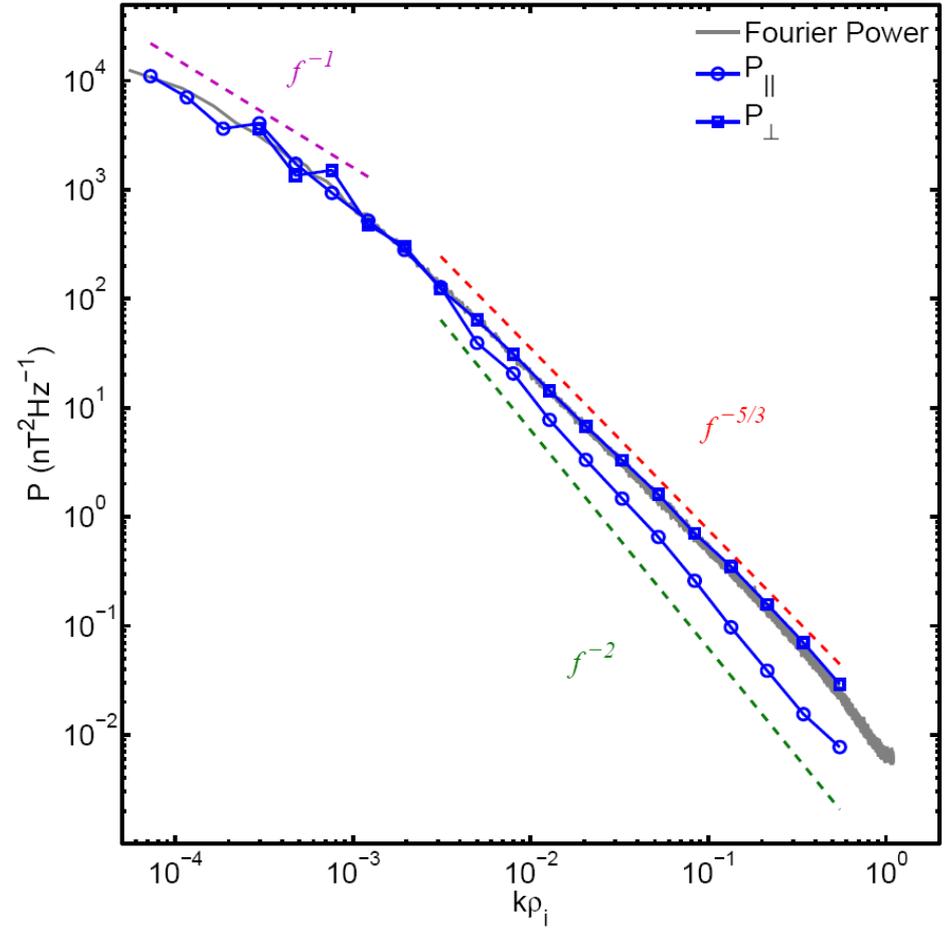
- For a given spacecraft frequency f , this corresponds to a flow-parallel scale $\lambda = V_{SW} / f$
- ...and a flow-parallel wavenumber $k_{\parallel} = 2\pi f / V_{SW}$
- But sensitive to all waves with $k \cdot V_{SW} = 2\pi f$



→ “reduced spectrum”

Power anisotropy

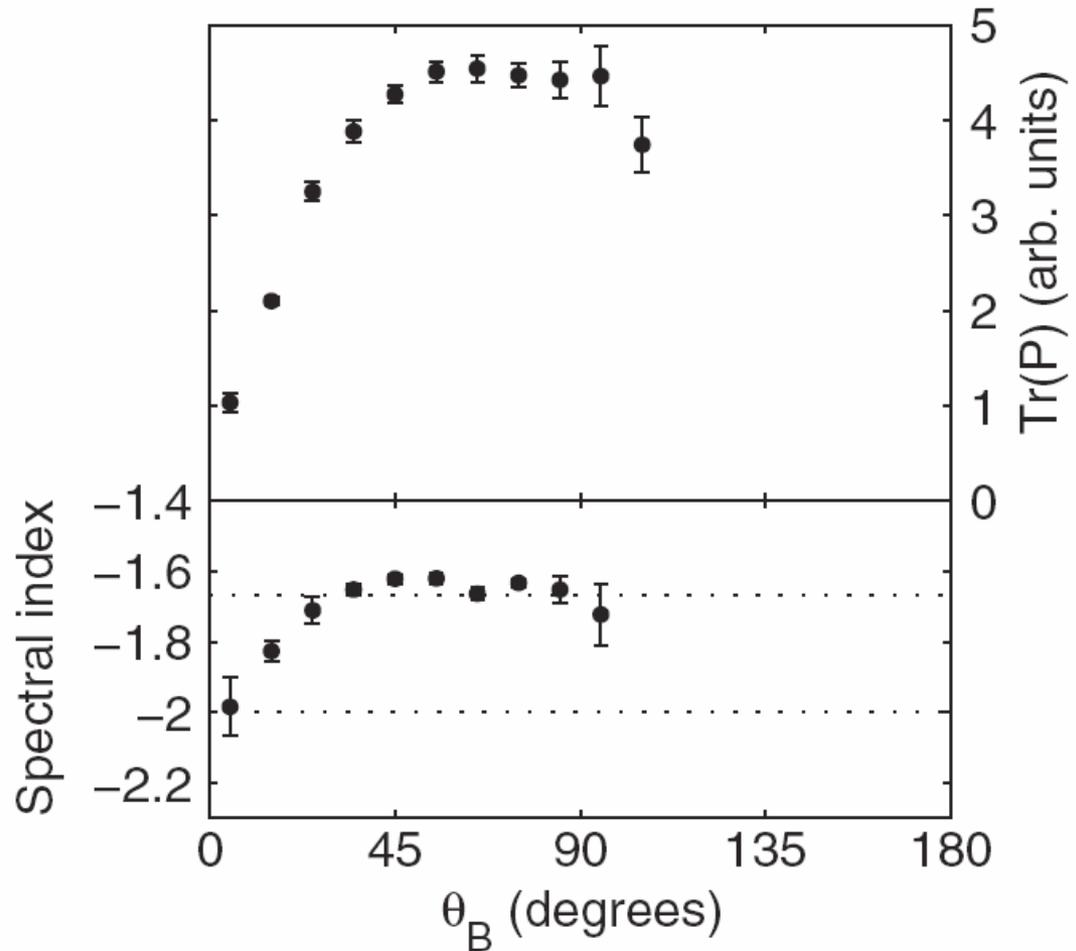
- Significant power anisotropy in the inertial range
- Power anisotropy seems to be generated through cascade
- Note: isotropy at the “outer scale”
- Wicks et al., Mon. Not. Roy. Astron. Soc., 2010



Consistency with critical balance

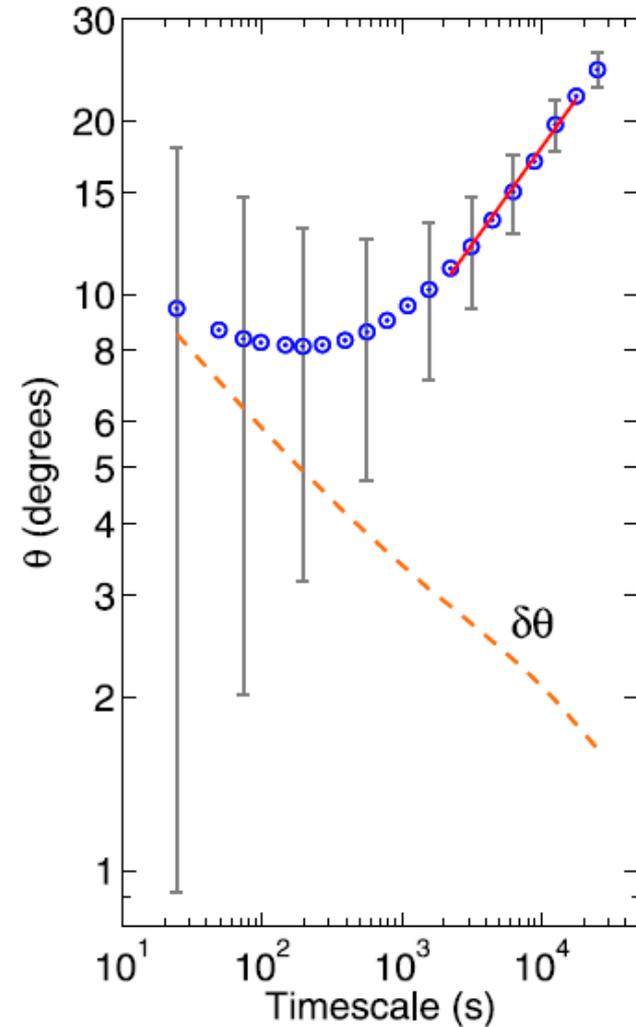
Inertial range

- $5/3$ spectral index perpendicular to field
- 2 spectral index parallel to field
- Consistent with critical balance
- Other explanations are possible!
- Horbury et al., 2008

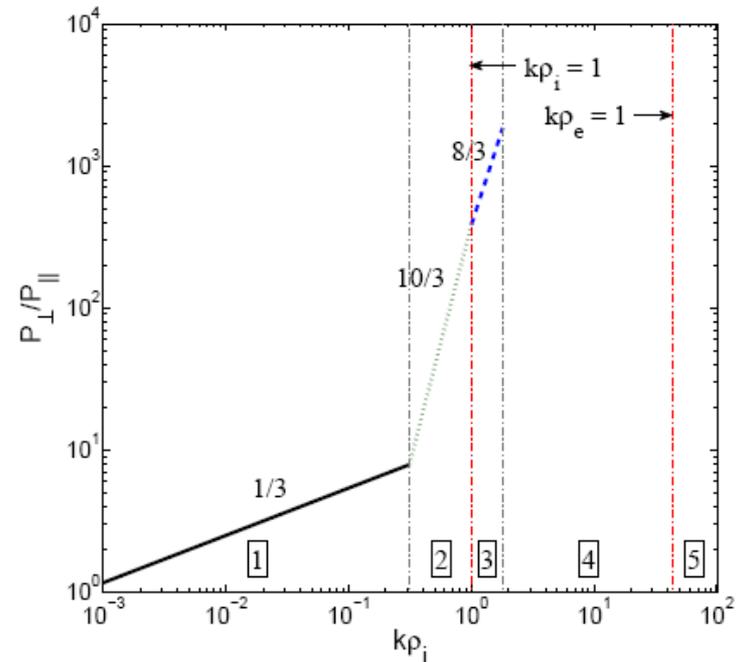
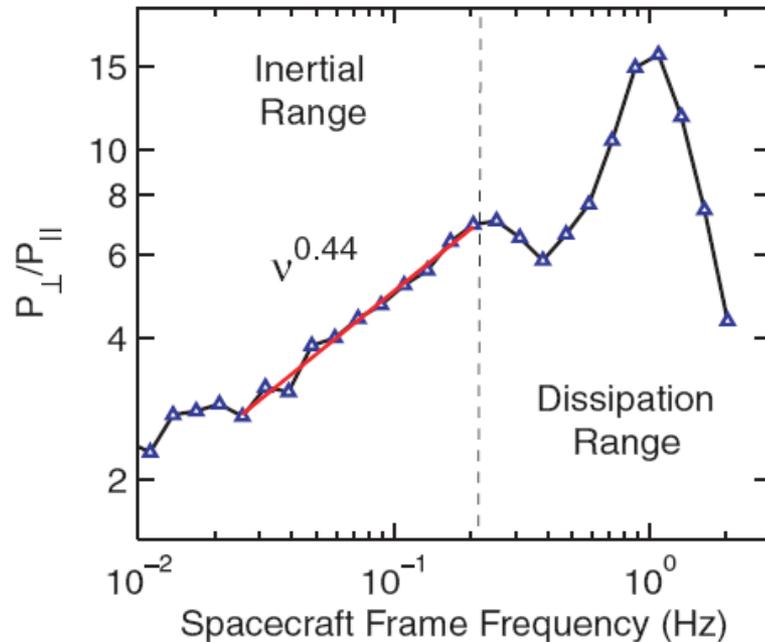


Dynamic alignment in the solar wind?

- Boldyrev, 2005
 - Angle between δb and δv should reduce down the cascade
- Podesta et al., J. Geophys. Res., A01107, 2009
 - Evidence for dynamic alignment in the solar wind?
- Timescale consistent with inertial range?



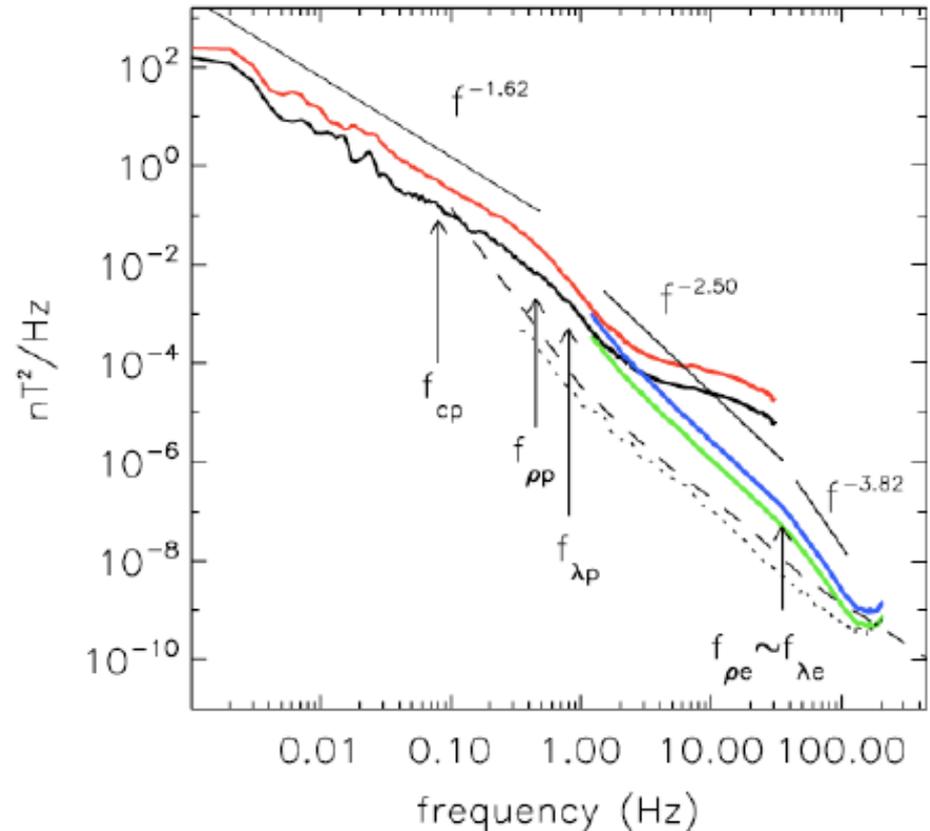
Transition to ion kinetic scales



- How does anisotropy vary across the transition to ion kinetics?
- Podesta, 2009: evidence for decreased anisotropy at ion gyroscale: instabilities?
- Chen et al., 2010: predictions for scaling based on CB gyrokinetic scalings

Kinetic effects

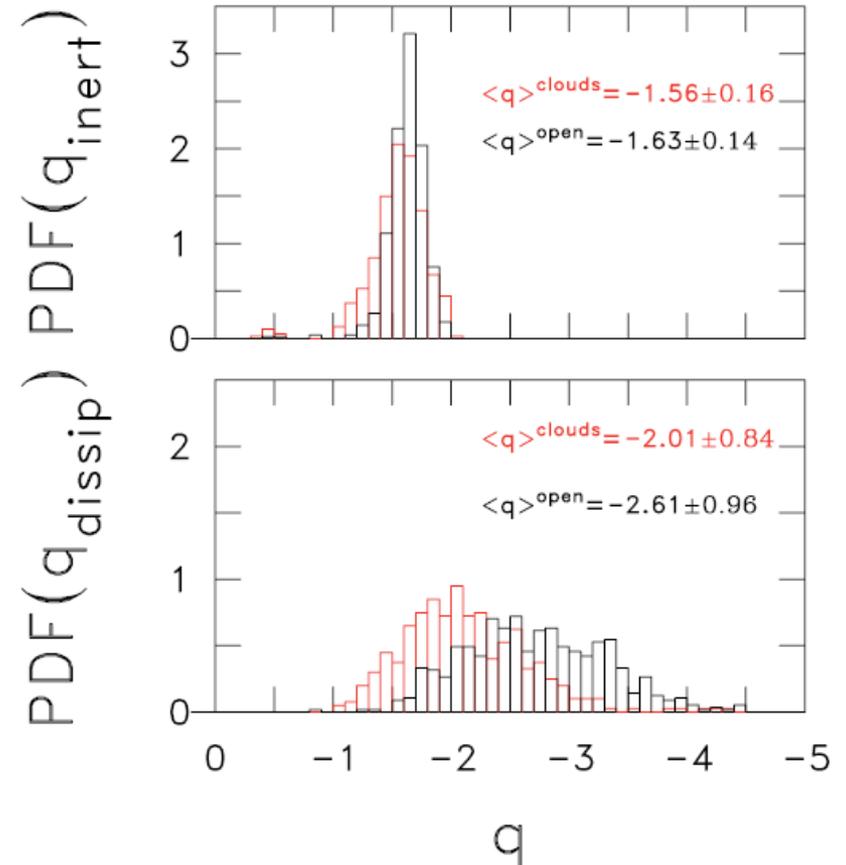
- Multiple possible dissipation mechanisms
 - Whistlers, kinetic Alfvén waves, ...
- Which one(s) is/are operating in the solar wind?
- Evidence for another power law at smaller scales
 - Continued energy transfer, not just dissipation



Sahraoui, 2009

Dispersion scale spectral index

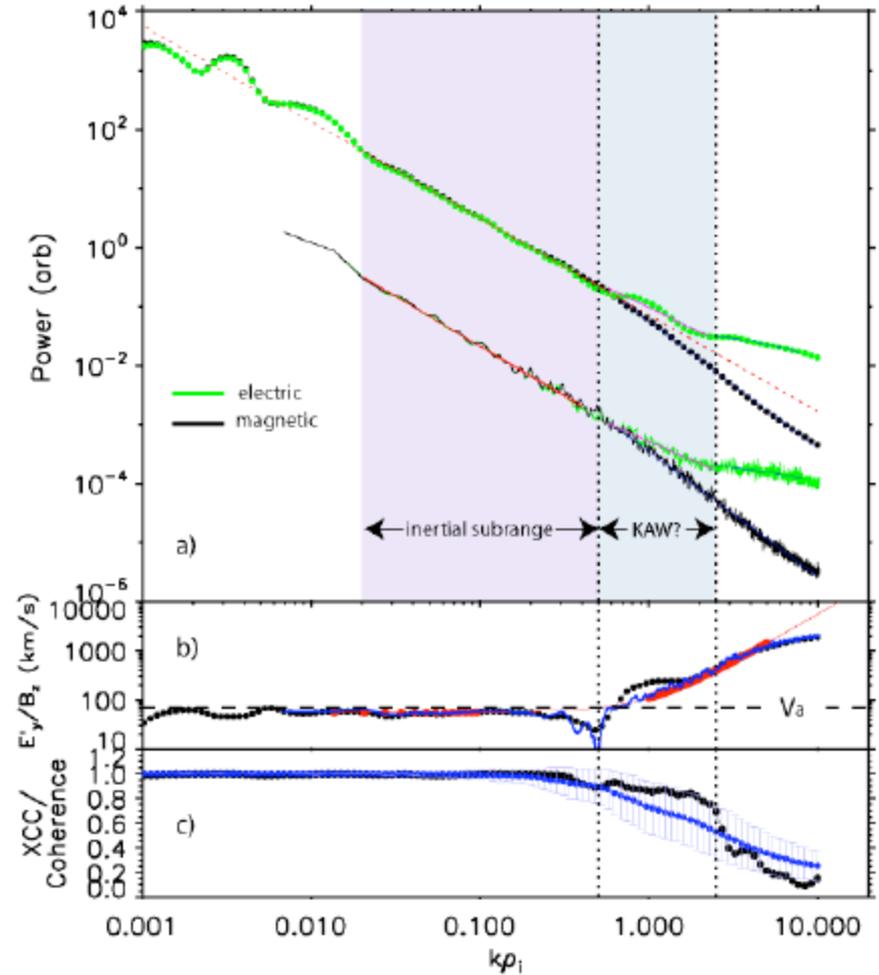
- MHD inertial range
 - Spectral index near $5/3$
- What happens in dissipation (dispersion?) range?
- Steeper spectrum
 - **Much more variable**



Smith et al., 2006

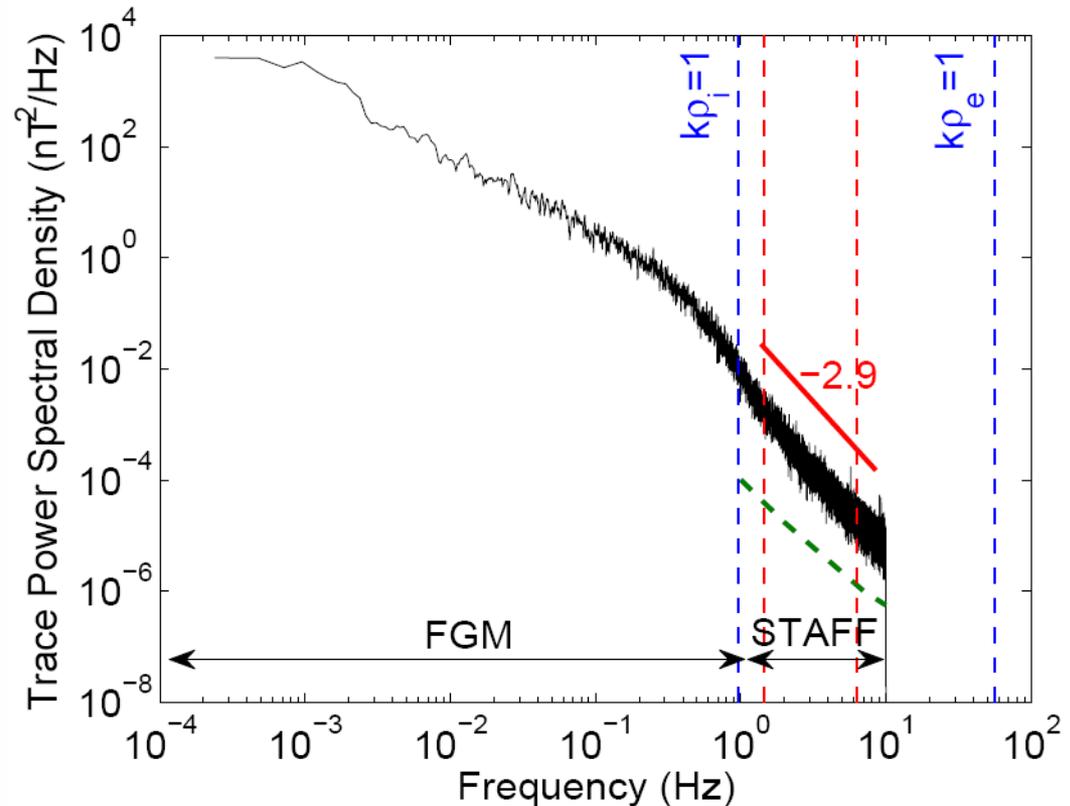
E and B spectrum in the kinetic regime

- Evidence for kinetic Alfvén waves?
- Bale, 2005



Dissipation scales with multi-spacecraft

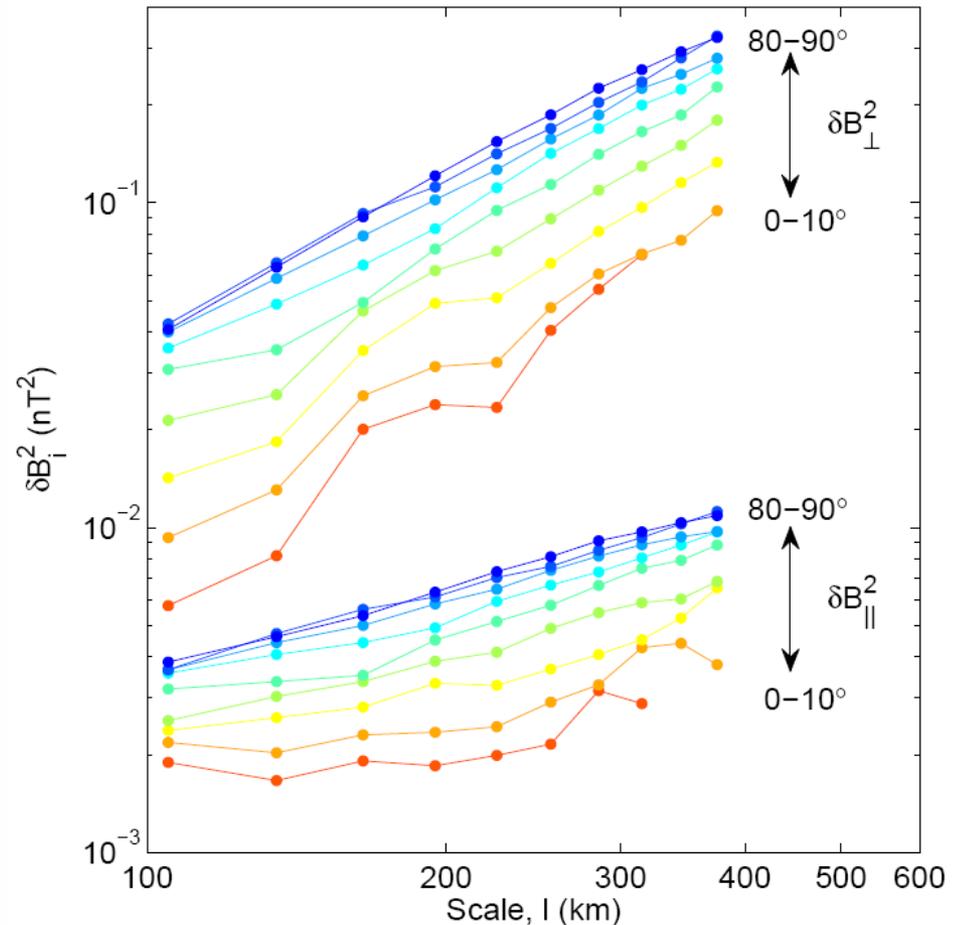
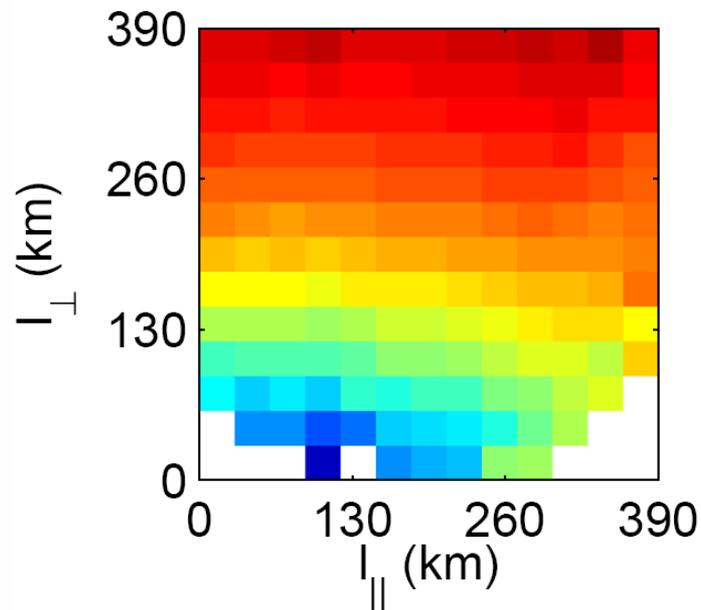
- Use four Cluster spacecraft on 100km scales
 - Provides information down to tens of km
- First measurement of power and spectral index anisotropy on dissipation scales



Chen et al., 2010

Multi-point structure functions

- Power law scaling on ion kinetic scales -> turbulent cascade
- Chen et al., PRL, 2010



Anisotropy on ion kinetic scales

- See power anisotropy similar to MHD scales

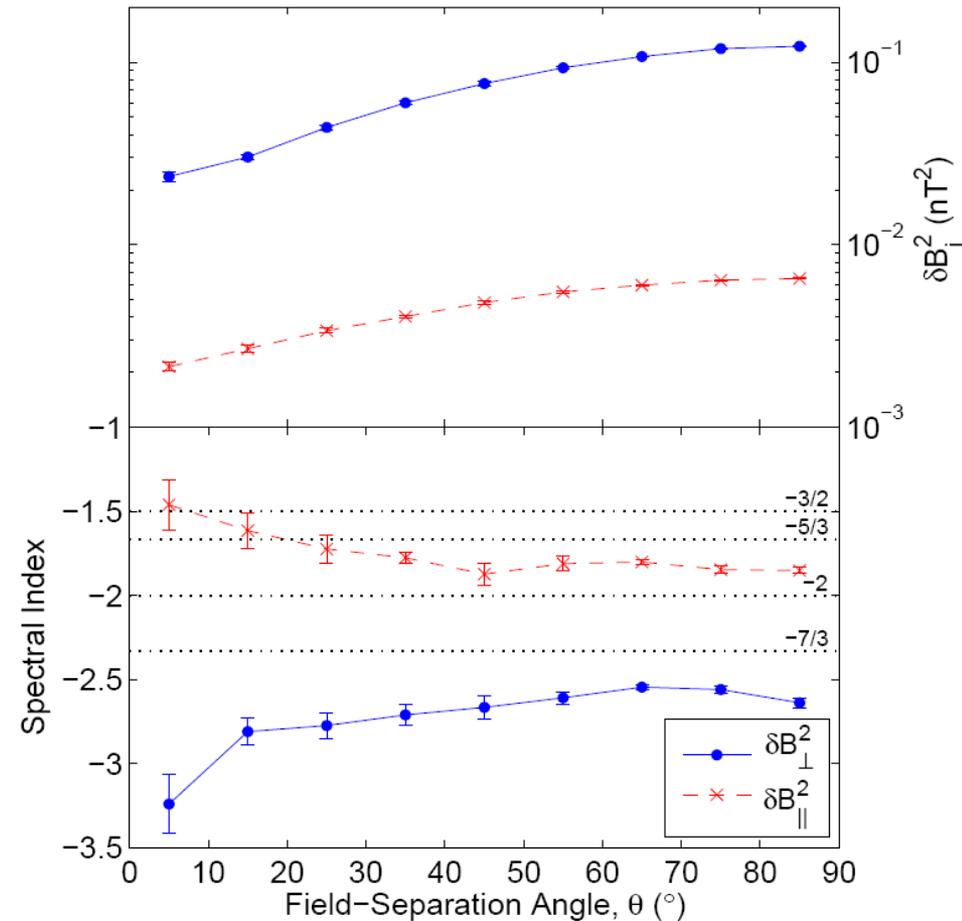
Field-perpendicular fluctuations

- Spectral index variations consistent with critically-balanced kinetic Alfvén waves

Field-parallel fluctuations

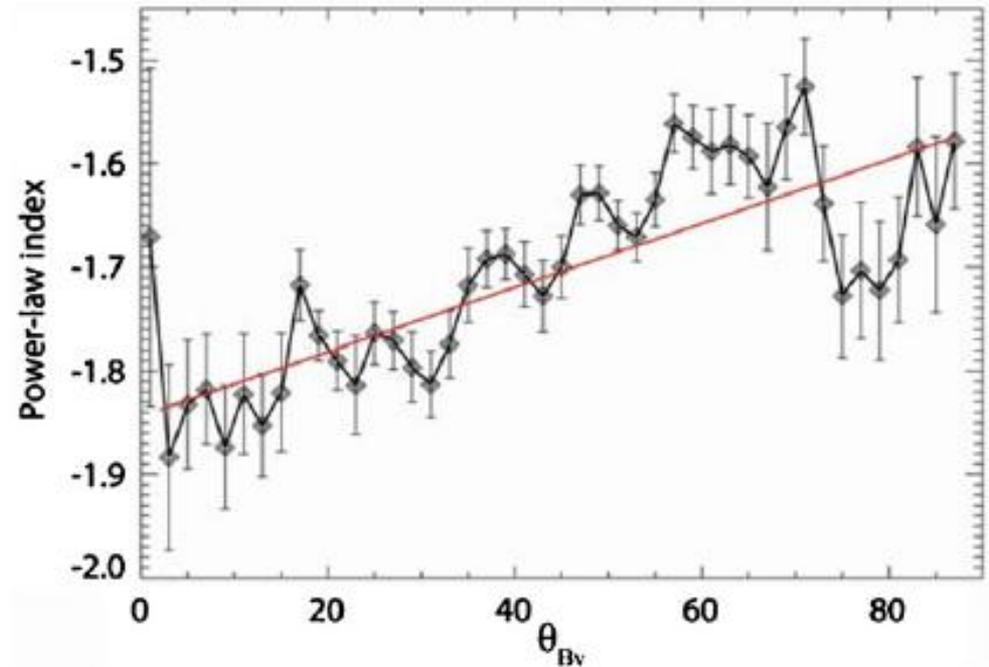
- Not consistent with critically-balanced kinetic Alfvén waves

Chen et al., PRL, 2010



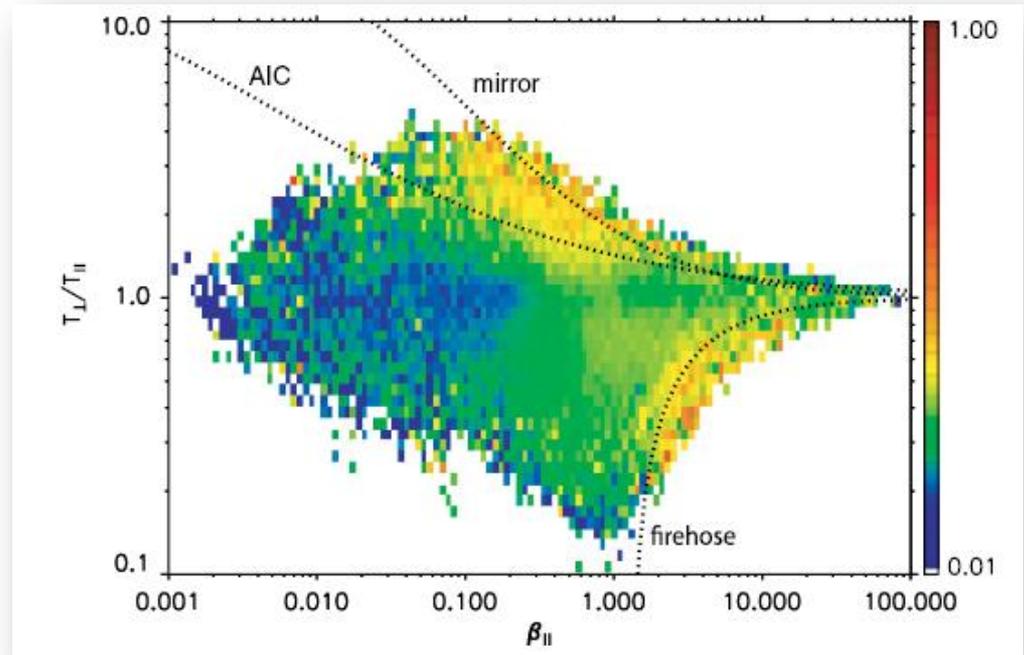
Anisotropic density scaling in the ion kinetic range

- Evidence for anisotropic scaling of density fluctuations
- Malaspina et al., 2010
- This is in the ion kinetic range
- Not consistent with theory?



Kinetic instabilities

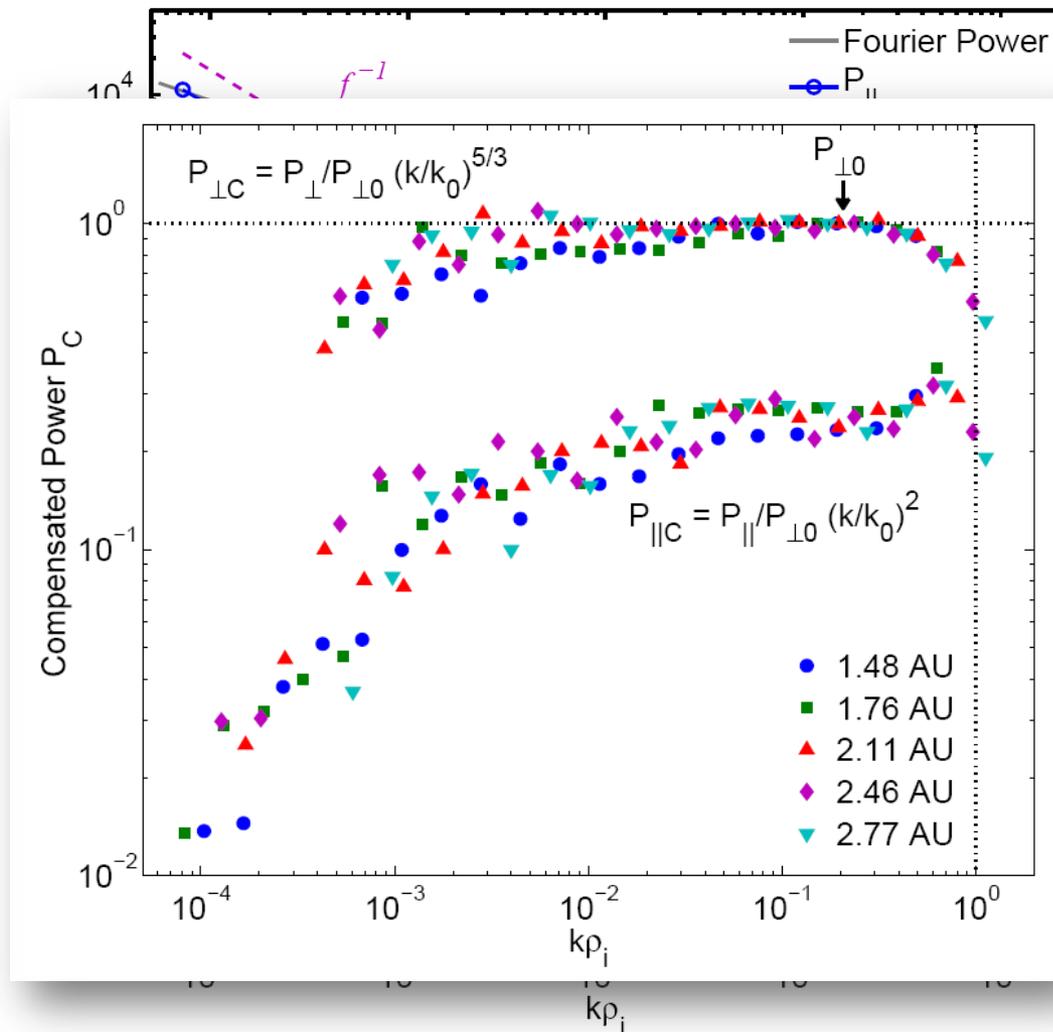
- Expansion of solar wind drives particle distributions towards firehose and mirror mode instabilities (Kasper, Hellinger, Matteini)
- Good evidence for generation of fluctuations on ion kinetic scales due to these
- See talks by Bale, Kasper



Bale et al., PRL, 2009

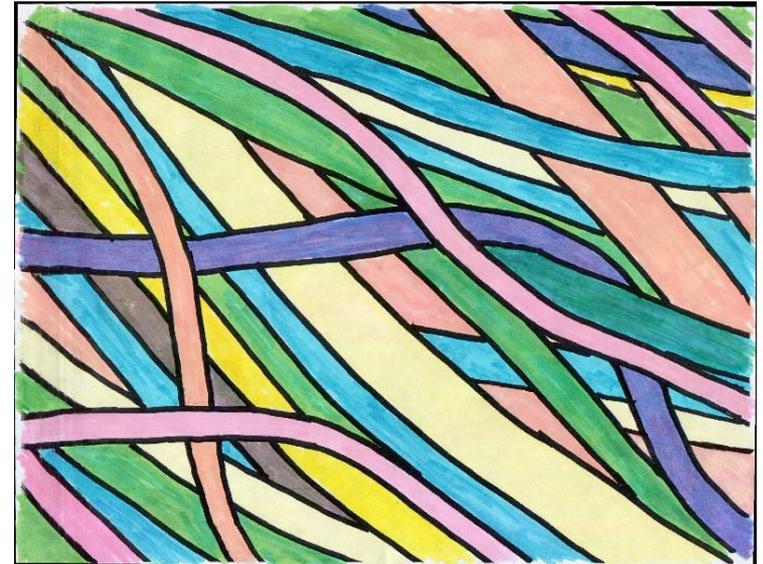
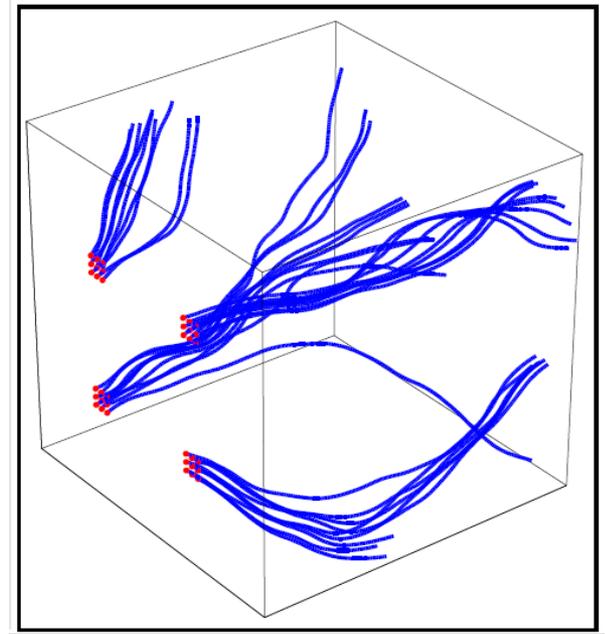
Evidence for firehose instability

- Consistent with plasma near firehose instability
- Appears to have field-parallel wavevector
- Only visible using wavelet analysis
- Wicks et al., MNRAS, 2010



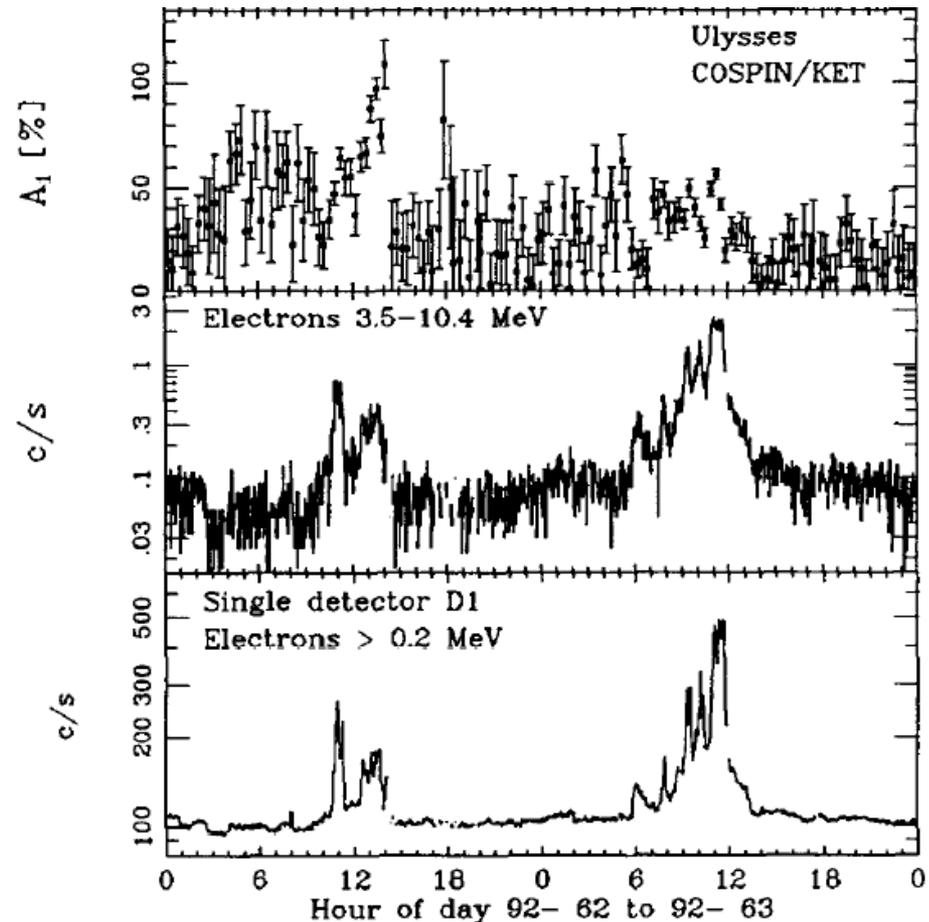
Discontinuities vs turbulence

- Turbulence
 - Field-perpendicular cascade generates short scales across the field
 - Tube-like structures
 - Not topological boundaries
- Flux tubes
 - Sourced from Sun
 - Topological boundary?
- Solar wind is likely a combination of both at the same time



Using particles to study turbulence

- Jovian electron bursts
 - Electrons highly tied to field lines
 - Relativistic electrons are instantaneous diagnostics of connectivity
 - Seen up to several hundred million km from planet
- Evidence for very fine scale structure



Ferrando et al., 1993

Summary and questions

- Anisotropic cascades on both MHD and ion kinetic scales
- Anisotropy in magnetic field, velocity and density, but some differences
- Evidence for kinetic instabilities, sometimes
- Imbalance is also sometimes present

Outstanding questions

- Is critical balance actually present on MHD or ion kinetic scales?
- What is the form of the ion kinetic cascade?
- What is the effect of imbalance?
- How important are instabilities and/or structures in solar wind dynamics?

